

# Distributed Detection of Randomly Located Targets in Mobility-Assisted Sensor Networks with Node Mobility Management

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## Abstract

Performance gain achieved by adding mobile nodes to a stationary sensor network for target detection, depends on factors such as the number of mobile nodes deployed, mobility patterns, speed and energy constraints of mobile nodes and the nature of the target locations (deterministic or random). In this paper, we address the problem of distributed detection of a randomly located target by a hybrid sensor network. Specifically, we develop two decision fusion architectures for detection where in the first one, impact of node mobility is taken into account for decisions updating at the fusion center while in the second model the impact of node mobility is taken at the node level decision updating. The cost of deploying mobile nodes is analyzed in terms of the minimum fraction of mobile nodes required to achieve the desired performance level within a desired delay constraint. Moreover, we consider managing node mobility under given constraints.

## I. INTRODUCTION

The problem of distributed detection and decision fusion in stationary wireless sensor networks has been extensively studied by many authors in different contexts [1]–[6]. However, stationary sensor networks may not suit for some applications, for example, in situations where it might be necessary to deploy a huge number of static nodes with limited coverage to monitor a large region within a desired performance level. In such situations, if relatively a small number of nodes are allowed to move, the system performance can be improved over time due to improvement in sensing coverage [7]. Deploying mobile nodes in a sensor network, however, may not be as cost effective as deploying static nodes. Also, nodes will have to spend

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node energy for mobility in addition to sensing and communication. Thus it is desirable to allow only a fraction of the nodes of the network to be mobile according to the requirement.

In this paper, we consider the problem of detecting a randomly located stationary target in a hybrid sensor network made of both mobile and static nodes. At the initial deployment stage, static and mobile nodes may scatter in the region of interest in random fashion, if the network does not have prior information about Phenomenon of Interest (PoI). Mobile nodes may be required to perform on-demand for different applications after the initial deployment. Due to energy constraints, we assume that the mobile nodes are kept stationary until a target is detected with certain confidence level, or useful statistics regarding the target locations are available. Note that since mobile nodes are required to perform on-demand for different functionalities, it is not possible to locate them in a certain area for a specific task. We assume that, at each time step, a mobile node can move to a limited number of locations from its current position, where these candidate locations are determined by physical factors related to mobile sensors and the environment. At each time step, mobile nodes move in a direction chosen based on the proposed mobility management schedule to maximize the detection probability during a desired delay constraint. At each time step, each node makes a local binary decision based on its observations and transmits it to the fusion center. The fusion center combines local decisions from all static and mobile nodes to reach at a final decision at the corresponding time instance. Specifically we develop two decision fusion models to make the final decision where in the first model, the impact of the node mobility is taken into account to update the decision at the fusion center, while in the second model, the impact of node mobility is taken at the node-level decisions. Since allowing more nodes to be mobile increases the cost, we characterize analytically, the required minimum fraction of mobile nodes to be directed to move in order to achieve a desired performance level within a desired delay constraint. We investigate the performance gain achieved by the hybrid sensor network when the network parameters are changing and discuss the scenarios where the node mobility is essentially improves the network performance.

The organization of the paper is as follows: Important related work is discussed in Section II. Section III explains the sensor network and the observation models, and presents the problem formulation. In Section IV, we develop a decision fusion model in which the fusion center updates the decisions over time while nodes make binary decisions based on the observations collected during one time step when the target location is random. Also, mobility management schedule is proposed to maximize the detection probability at the fusion center within a desired delay constraint. In this discussion, the effect of the node mobility is taken into account at the fusion center decision updating. In Section V a decision fusion model is developed in which the effect of the node mobility is taken into account at the node-level decisions. In Section VI, we develop an analytical procedure to find the minimum number of mobile nodes that should be incorporated with static nodes to achieve a desired performance level within a desired delay constraint.

Performance results are given in Section VII and the concluding remarks are given in Section VIII.

## II. RELATED WORK

Distributed detection and decision fusion is analyzed by many authors in different contexts, for example, [1]–[6], [8]–[10], to name a few. However, many of these existing analysis on target detection have considered stationary sensor networks, where sensor nodes are deployed with fixed positions or in a random fashion. Since the performance of such a stationary sensor network is limited by network size, sensing ranges, etc., recently mobile sensor nodes in wireless sensor network applications have been suggested to enhance the system performance [7].

Use of node mobility in mobile sensor networks for relocation after initial random placement was previously suggested in [11], [12]. However, in their models, nodes only make a one-time movement to achieve a better (uniform) coverage. Using mobile nodes as data collection points (sinks) in sensor networks was studied by [13]–[15]. Liu et. al. in [7] showed that the coverage can be improved by a mobile sensor network with continuous mobility over the time compared to that with a static network. Surveillance coverage of mobile sensor networks under Brownian motion random node mobility model was addressed in [16]. Managing mobile node mobility in target tracking applications in mobile sensor networks is addressed in [17].

Since deploying mobile nodes for continuous performance (coverage, detection and tracking) improvement might not be as cost effective as deploying static nodes, it is useful to consider networks consisting of both static and mobile nodes where the mobile nodes are allowed to move only if necessary. The target tracking performance of an integrated mobile-static sensor network was addressed in [18]. In [18], the mobile nodes are used to aid the data propagation when the communication ranges of static nodes are limited. The target detection in a hybrid sensor network is addressed by [19], [20] where they have proposed a two phase detection model for target detection assuming known target locations. Although we address a similar problem, our work is different from [19], [20] in several contexts. (i). In this paper we explicitly present two decision fusion models for target detection when the target location is random. (ii). We consider constrained mobility for mobile nodes where each node can move only in a pre-determined set of candidate directions from their current locations. (iii). We evaluate the cost of deploying mobile nodes in terms of the minimum fraction of mobile nodes that should be directed to move to achieve a desired performance level within a desired delay constraint, analytically. Moreover, [19], [20] did not allow for the possibility of imperfect communication links between nodes and the fusion center.

## III. PROBLEM FORMULATION AND SYSTEM MODEL

We consider a hybrid sensor network made of  $N$  number of total sensors. We assume that there is  $N_s$  number of static nodes and a maximum of  $N_m$  number of mobile nodes initially deployed in a square

region with dimensions  $b \times b$ . Note that when mobile nodes are not in the mobile configuration, they make measurements at their stationary configuration. Denote  $\lambda_m = \frac{N_m}{N}$  and  $\lambda_s = \frac{N_s}{N}$  to be the fractions of mobile and static nodes, respectively. Denote  $(x_{sk}, y_{sk})$  to be the location of the  $k$ -th static node which is assumed to be fixed after initial deployment. Let  $\mathcal{V}$  be the set of all node indices in the network and let  $\mathcal{V}_m$  and  $\mathcal{V}_s$  to be the sets containing mobile and static node indices, respectively.

### A. Problem formulation

In this paper, we assume that the network is kept stationary until a target is detected at a certain confidence level. We also assume that the network does not have any information regarding sensing field at the time of deployment. Information regarding possible target locations may be available to the network after initial deployment and, the target can be appeared in a particular target location during a certain period of time. Because of these factors, it is not possible to deploy mobile sensors to cover possible target locations at the time of deployment, and on the other hand, mobile nodes may be required to perform on-demand for different purposes. The key contributions in this paper are three-fold.

- 1) Develop decision fusion architectures for the target detection by hybrid sensor network when the target location is random. Specifically, we propose two decision fusion architectures where in the first one, the effect of the node mobility is taken into account for the decision updating at the fusion center and nodes make binary decisions based on the observations during one step movement. In the second model, nodes take the effect of the node mobility into account for node-level decision updating.
- 2) Manage node mobility to improve (maximize) the system performance within a desired delay constraint after a target is initially detected by the stationary configuration at certain confidence level.
- 3) The cost of mobile nodes is evaluated in terms of the minimum number of mobile nodes required to achieve a desired performance level within a desired delay constraint.

### B. Node mobility model

We assume limited mobility of mobile nodes where at each time step each mobile node can only move in one of the pre-determined set of locations (or directions) as shown in Fig. 1 (for example), and the maximum total distance it can move in any direction is bounded. This mobility model is justifiable in cases where a node can move to a limited number of locations from its current position due to terrain constraints. Let the velocity of mobile node  $k$  at time  $t$  be  $\mathbf{v}_k(t) = (v_k(t), \theta_k(t)) = (v_k, \theta_k(t))$  where  $v_k(t) = v_k$  is the speed of the node  $k$  that is assumed to be constant and  $\theta_k(t)$  is the direction of node  $k$  at time  $t$ . Denote  $l_{max}^k$  is the maximum distance that the  $k$ -th mobile node can move with the available

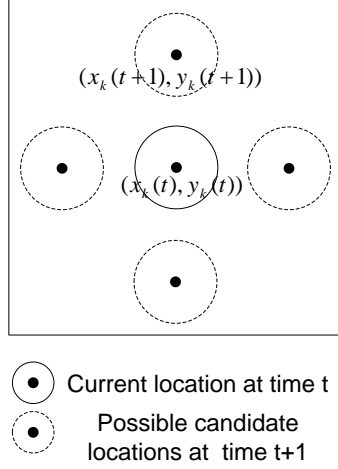


Fig. 1. Candidate locations for a mobile node at time  $t$

resources. At each time step  $T_s$ , mobile node  $k$  moves with an average speed of  $v_k$  in a direction  $\theta_k$  selected from a set  $\Theta = \{\theta^1, \theta^2, \dots, \theta^K\}$ . Selection of  $\theta_k$  at each time step  $T_s$  is considered in later sections. Let  $(x_k(t), y_k(t))$  denote the location of the  $k$ -th mobile node at time  $t$ . Under this mobility model, the location  $(x_k(t), y_k(t))$  of the  $k$ -th mobile node at time  $jT_s \leq t \leq (j+1)T_s$  is given by

$$\begin{aligned} x_k(t) &= x_k(jT_s) + (t - jT_s)v_k \cos \theta_k(jT_s) \\ y_k(t) &= y_k(jT_s) + (t - jT_s)v_k \sin \theta_k(jT_s), \end{aligned}$$

for  $k \in \mathcal{V}_m$ , and  $j = 0, 1, 2, \dots$ , where  $\theta_k(jT_s) \in \Theta$  is the selected direction at time  $jT_s$  and  $(x_k(0)$  and  $y_k(0))$  are  $X$  and  $Y$  coordinates of the initial location of the  $k$ -th mobile node.

### C. Observation model

At each time step both mobile and static nodes make observations on the presence/absent of the target and make a binary decision on whether the target is present or absent. We consider the observation models for mobile and static nodes as given below at time  $0 < t \leq nT_s$  under hypotheses  $\mathcal{H}_1$  (target present) and  $\mathcal{H}_0$  (target absent):

$$\begin{aligned} \mathcal{H}_1 &: z_k(t) = m_k(t) + u_k(t); \text{ for } 0 < t \leq nT_s, \\ \mathcal{H}_0 &: z_k(t) = u_k(t); \text{ for } 0 < t \leq nT_s, \end{aligned} \quad (1)$$

for  $k \in \mathcal{V}$ , where  $\{m_k(t), t \in (0, nT_s]\}$  is the signal strength received from the target at time  $t$ ,  $\{u_k(t), t \in [0, nT_s]\}$  is the measurement noise process at the  $k$ -th node which is assumed to be white Gaussian with

mean zero and the auto-covariance function  $C_n(t1, t2) = \sigma_u^2 \delta(t1 - t2)$ ,  $t1, t2 \in [0, nT_s]$  where  $\delta(\cdot)$  denotes the Dirac delta function.

The received sensing signal  $m_k(t)$  represents the attenuated (over distance) signal emitted by the target. Depending on the sensing modalities, (such as acoustic, seismic, IR, etc..), different models for received signal strength can be used. For this discussion, we assume the following model for the signal  $m_k(t)$ , which assumes that the signal emitted by the target decays as the distance from the target to the sensing node increases [2], [21]:

$$m_k(t) = \frac{A_0}{r_k^{a/2}(t)}, \text{ for } 0 \leq t \leq nT_s, k \in \mathcal{V}_m \quad (2)$$

where  $A_0$  is the signal strength emitted by the target,  $r_k(t) = \sqrt{(x_k(t) - x_0)^2 + (y_k(t) - y_0)^2}$  is the distance between the  $k$ -th mobile node and the target at time  $t$  for  $0 \leq t \leq nT_s$ ,  $(x_0, y_0)$  is the location of the stationary target and  $a$  is the path loss index that is assumed to be 2 throughout. Note that, for static nodes (2) reduces to

$$m_k(t) = \frac{A_0}{r_k^{a/2}}, k \in \mathcal{V}_s, \quad (3)$$

where  $r_k = \sqrt{(x_{sk} - x_0)^2 + (y_{sk} - y_0)^2}$ . However, the results presented in this paper can be generalized to other sensing modalities as well.

#### IV. DETECTION PERFORMANCE WITH DECISION FUSION ARCHITECTURE 1: FUSION CENTER UPDATING DECISIONS OVER TIME

In this section we consider the performance dynamics of the hybrid sensor network when the exact target location is unknown. At the stationary configuration, we assume that the network monitors the Field of Interest (FoI) continuously, and mobile nodes are directed to move when a possible target is detected with relatively lower confidence level by the stationary configuration. More precisely let  $P_D^0$  and  $P_F^0$  be the overall (system) detection and false alarm probabilities at time  $t = 0$ . If  $P_D^0 \geq \epsilon_1$  and  $P_F^0 \leq \epsilon_2$ , for particular  $\epsilon_1$  and  $\epsilon_2$ , we say that a target is detected at time zero with a low confidence level. The target location coordinates,  $x_0$  and  $y_0$  are assumed to be random variables with known statistics. Moreover, in this work we assume that once appeared, the target remains active for a known period of time.

After initially detected by a lower confidence level, we assume that mobile and static nodes make binary decisions at each time instant  $nT_s$  for  $n = 1, 2, \dots$  based on the observations collected during the current time interval. Formally, the  $k$ -th node performs the following hypothesis testing problem at time  $t = nT_s$ :

$$\begin{aligned} \mathcal{H}_1 & : z_k(t) = m_k(t) + u_k(t); \text{ for } (n-1)T_s < t \leq nT_s, \\ \mathcal{H}_0 & : z_k(t) = u_k(t); \text{ for } (n-1)T_s < t \leq nT_s \end{aligned} \quad (4)$$

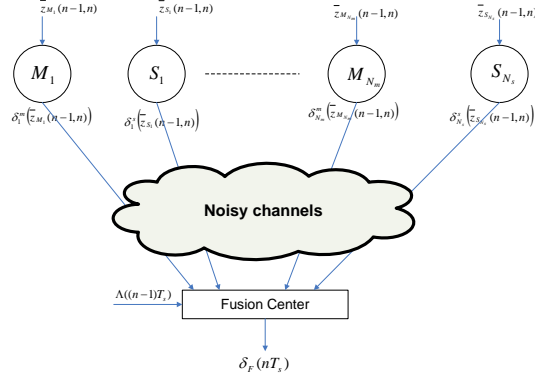


Fig. 2. Decision Fusion Architecture for the Hybrid Sensor Network with Fusion Center updating Decisions over Time

Each node transmits its local decision to the fusion center over a noisy communication channel. The fusion center combines these local decisions from mobile and static nodes and the previous information at the fusion center to make a final decision. The corresponding decision fusion architecture is shown in Fig. 2 where the symbols used in Fig. 2 are defined in subsections IV-A and IV-C. As shown in Fig. 2, at each time instant  $nT_s$ , each node performs a local detection based on the observations collected at the current time interval  $(n-1)T_s \leq t < nT_s$ . The corresponding local decisions are transmitted to the fusion center over a noisy communication channel at each time step  $t = nT_s$ . The fusion center updates the final decision based on the noisy corrupted decisions received from both static and mobile nodes at time  $nT_s$ , and the previous information at the fusion center at time  $(n-1)T_s$  to reach a final decision. In this architecture, the impact of the mobility of mobile nodes is taken into account at the fusion center while the mobile nodes make a local decision based on observations collected at one-step movement.

#### A. Detection performance at $k$ -th mobile node

Denote  $z_k(t; n-1, n) = (z_k(t))_{t=(n-1)T_s}^{nT_s}$ . Note that according to the signal model (2) assumed in the paper, the signal strength received by a sensor node is decreasing as the distance between the node location and the target location is increasing. If a simple constant threshold testing is performed on the received signal strength [2] (or on energy [20]) at a sensor node to determine the target is present/absent, it can be seen that more false alarms will occur at the nodes located relatively far away from the target location if the threshold is chosen too small, or miss probability will be higher at sensors located closer to the target location, if the threshold is too large. [2] has provided an approach of selecting an optimal threshold such that the performance at the fusion center is maximized for a static sensor network. However, in this paper since mobile nodes are directed to move when required, maintaining a constant threshold test on signal strength (or energy) to determine the presence/absence of a target would not essentially reflect the performance gain achieved by node mobility. Thus it is required to have a dynamically varying threshold

at sensor nodes to exploit the impact of node mobility in an effective way. Thus, in this paper we consider that  $k$ -th mobile node to perform likelihood ratio testing on its observations. Explicitly we assume that each node performs  $\alpha_1$  ( $\leq P_F^0$ )-level Neyman-Pearson (N-P) optimum test to detect the presence/absence of the target at each time  $nT_s$ , since the ultimate goal in this paper is to manage node mobility to result optimal detection probability.

According to the detection problem at the  $k$ -th mobile node as given by (4), the log likelihood ratio based on the observations collected during time interval  $((n-1)T_s, nT_s]$ ,  $L_k(z_k(t; n-1, n))$ , conditioned on the target location  $(x_0, y_0)$ , at the  $k$ -th mobile node can be shown to be [22],

$$\begin{aligned}
& L_k(z_k(t; n-1, n)|(x_0, y_0)) \\
&= \log \frac{dP_1}{dP_0}(z_k(t; n-1, n)) \\
&= \frac{1}{\sigma_u^2} \int_{(n-1)T_s}^{nT_s} m_k(t; x_0, y_0) z_k(t) dt \\
&\quad - \frac{1}{2\sigma_u^2} \int_{(n-1)T_s}^{nT_s} m_k^2(t; x_0, y_0) dt, \\
&= \frac{\tilde{z}_k(n-1, n)}{\sigma_u^2} - \frac{E_k^m(n-1, n)}{2\sigma_u^2}, \tag{5}
\end{aligned}$$

for  $k \in \mathcal{V}_m$  where  $\tilde{z}_k(l, n) = \int_{lT_s}^{nT_s} m_k(t; x_0, y_0) z_k(t) dt$  and  $E_k^m(l, n) = \int_{lT_s}^{nT_s} m_k^2(t; x_0, y_0) dt$  for  $n = 1, 2, \dots$  and  $m_k(t; x_0, y_0) = \frac{A_0}{\sqrt{(x_k(t)-x_0)^2+(y_k(t)-y_0)^2}}$  as defined in (2). Computation of  $E_k^m(l, n)$  for a given target location is given in subsection V-A. Then the log likelihood ratio  $L_k(z_k(t; n-1, n))$  is given by,

$$\begin{aligned}
& L_k(z_k(t; n-1, n)) \\
&= \mathbb{E}_{x_0, y_0} \left\{ \frac{\tilde{z}_k(n-1, n)}{\sigma_u^2} - \frac{E_k^m(n-1, n)}{2\sigma_u^2} \right\} \\
&= \frac{1}{\sigma_u^2} \int_{(n-1)T_s}^{nT_s} z_k(t) \overline{m_k(t)} dt - \frac{1}{2\sigma_u^2} \overline{E_k^m(n-1, n)} \tag{6}
\end{aligned}$$

where  $\overline{m_k(t)} = \mathbb{E}_{x_0, y_0} \{m_k(t; x_0, y_0)\}$  and  $\overline{E_k^m(n-1, n)} = \mathbb{E}_{x_0, y_0} \{E_k^m(n-1, n)\}$ . Computation of  $\overline{m_k(t)}$  is associated with the specific probabilistic model for the target location distribution. For the evaluation used in this paper, the closed-form expression for  $\overline{m_k(t)}$  with assumed target location distribution model is given in Section VII. Assuming no point masses in the pdf of  $L_k(z_k(t; n-1, n))$ , the optimal decision rule at the  $k$ -th mobile node at time  $t = nT_s$  for the hypothesis problem (4) is given by (according to the N-P-criteria [22])

$$\delta_k^m(nT_s) = \begin{cases} 1 & \geq \\ \text{if } L_k(z_k(t; n-1, n)) & \eta_k^m(n) \text{ ,} \\ 0 & < \end{cases} \tag{7}$$



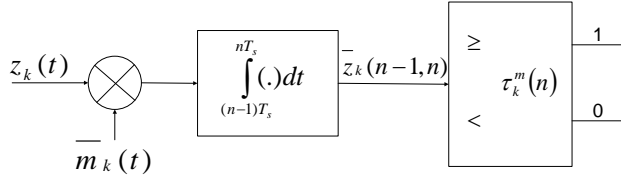


Fig. 3. Detector structure at the  $k$ -th mobile node for the decision making based on the observations during time interval  $((n-1)T_s, nT_s]$

where  $\eta_k^m(n) \geq 0$  is uniquely determined such that, the false alarm probability (f.a.p.) at the  $k$ -th node at time  $nT_s$ ,  $P_{f_k}^m(nT_s) = \alpha_1$  for  $k \in \mathcal{V}_m$ . Note that we assume that each node performs same  $\alpha_1$ -level N-P test at each time  $nT_s$ . The decision rule (7) can be further simplified to,

$$\delta_k^m(nT_s) = \begin{cases} 1 & \geq \\ \text{if } \bar{z}_k(n-1, n) & \tau_k^m(n) \\ 0 & < \end{cases}, \quad (8)$$

where  $\bar{z}_k(n-1, n) = \int_{(n-1)T_s}^{nT_s} z_k(t) \overline{m_k(t)} dt$  is the new decision statistic and  $\tau_k^m(n) = \sigma_u^2 \eta_k^m(n) + \frac{1}{2} \bar{E}_k^m(n-1, n)$  is the new threshold, at the  $k$ -th mobile node for  $k \in \mathcal{V}_m$ .

*Proposition 1:* For  $\alpha_1$ -level N-P test, the threshold  $\tau_k^m(n)$  and the detection probability at the  $k$ -th mobile node at time  $nT_s$  are given by,

$$\tau_k^m(n) = \sigma_u Q^{-1}(\alpha_1) \sqrt{E_k^{\bar{m}}(n-1, n)} \quad (9)$$

and

$$\bar{P}_{d_k}^m(nT_s) = \mathbb{E}_{x_0, y_0} \left\{ Q \left( Q^{-1}(\alpha_1) - \frac{\tilde{E}_k(x_0, y_0; n-1, n)}{\sigma_u \sqrt{E_k^{\bar{m}}(n-1, n)}} \right) \right\} \quad (10)$$

respectively, where  $\tilde{E}_k(x_0, y_0; n-1, n) = \int_{(n-1)T_s}^{nT_s} m_k(t; x_0, y_0) \overline{m_k(t)} dt$  and  $E_k^{\bar{m}}(n-1, n) = \int_{(n-1)T_s}^{nT_s} \overline{m_k^2(t)} dt$ . The  $Q(\cdot)$  function is defined as  $Q(x) = \frac{1}{\sqrt{2\pi}} \int_x^\infty e^{-\frac{t^2}{2}} dt$ .

The proof of the Proposition 1 is given in Appendix A. The block diagram of the detector at the  $k$ -th mobile node is shown in Fig. 3.

### B. Detection performance at $k$ -th static node

*Proposition 2:* For static nodes, the optimal threshold and the detection probability for the  $\alpha_1$ -level N-P test are given by,

$$\tau_k^s(n) = \tau_k^s = \sigma_u Q^{-1}(\alpha_1) \bar{m}_k \sqrt{T_s} \quad (11)$$

and

$$\bar{P}_{d_k}^s(nT_s) = \mathbb{E}_{x_0, y_0} \left\{ Q \left( Q^{-1}(\alpha_1) - \frac{m_k(x_0, y_0) \sqrt{T_s}}{\sigma_u} \right) \right\}. \quad (12)$$

See Appendix B for the proof of the Proposition 2. Note that the detection threshold  $\tau_k^s$  for a static node is a constant over the time.

### C. Performance evaluation at fusion center with noisy communication

To evaluate the performance of the hybrid sensor network, let us assume that the nodes send their local decisions to the fusion center over binary symmetric channels (BSC) which can be used to model noisy channels [2], [23]. Denote  $w_k(nT_s)$  to be the received signal at the fusion center from the  $k$ -th node at time  $t = nT_s$  for  $n = 0, 1, 2, \dots$ . Note that at  $t = 0$ , the decision center has agreed that a target is detected at a lower confidence level if  $P_D^0 \geq \epsilon_1$  and  $P_F^0 \leq \epsilon_2$ . Thus at time  $t = 0$ , the fusion center has the decision, under  $\mathcal{H}_1$ ,  $w(0) = 1$  with probability  $P_D^0$  and  $w(0) = 0$  with probability  $1 - P_D^0$ . Similarly, under  $\mathcal{H}_0$ ,  $w(0) = 1$  with probability  $P_F^0$  and  $w(0) = 0$  with probability  $1 - P_F^0$ . For  $n \geq 1$ , we assume that the  $k$ -th node transmits its local decision over a BSC with a cross-over probability  $p_k$ , and that the channels of  $N$  nodes are independent of each other. The received signals at the fusion center under the two hypotheses at time  $nT_s$  for  $n = 1, 2, \dots$  are given by

$$\begin{aligned} w_k(nT_s) &= \begin{cases} 1 & \text{with } \mu_{d_k}^m(nT_s) \\ 0 & \text{with } 1 - \mu_{d_k}^m(nT_s) \end{cases} \text{ for } k \in \mathcal{V}_m \\ &= \begin{cases} 1 & \text{with } \mu_{d_k}^s(nT_s) \\ 0 & \text{with } 1 - \mu_{d_k}^s(nT_s) \end{cases} \text{ for } k \in \mathcal{V}_s \end{aligned} \quad (13)$$

under  $\mathcal{H}_1$  and

$$\begin{aligned} w_k(nT_s) &= \begin{cases} 1 & \text{with } \mu_{f_k}^m(nT_s) \\ 0 & \text{with } 1 - \mu_{f_k}^m(nT_s) \end{cases} \text{ for } k \in \mathcal{V}_m \\ &= \begin{cases} 1 & \text{with } \mu_{f_k}^s(nT_s) \\ 0 & \text{with } 1 - \mu_{f_k}^s(nT_s) \end{cases} \text{ for } k \in \mathcal{V}_s \end{aligned} \quad (14)$$

under  $\mathcal{H}_0$  where for  $n = 1, 2, \dots$ ,  $\mu_{d_k}^m(nT_s) = \bar{P}_{d_k}^m(nT_s)(1 - p_k) + (1 - \bar{P}_{d_k}^m(nT_s))p_k$ ,  $\mu_{d_k}^s(nT_s) = \bar{P}_{d_k}^s(nT_s)(1 - p_k) + (1 - \bar{P}_{d_k}^s(nT_s))p_k$ ,  $\mu_{f_k}^m(nT_s) = \alpha_1(1 - p_k) + (1 - \alpha_1)p_k$  and  $\mu_{f_k}^s(nT_s) = \alpha_1(1 - p_k) + (1 - \alpha_1)p_k$ .

For the fusion center to perform optimal fusion rule, it should have the knowledge of detection and false alarm probabilities of local nodes at each time step. Although local false alarm probabilities can be easily made available at the fusion center since they are the same at each node and do not change with time, the analogy is not convenient with local detection probabilities. Thus in this paper, we assume that the fusion center makes a final decision at time  $t = nT_s$  using the counting rule based on the received signals from all nodes at time  $nT_s$  and the previous available at the fusion center at time  $(n-1)T_s$ . Denote

the decision statistic at the fusion center to be  $\Lambda(nT_s)$ , where

$$\Lambda(nT_s) = \left( \Lambda((n-1)T_s) + \sum_{k \in \mathcal{V}_m} w_k(nT_s) + \sum_{k \in \mathcal{V}_s} w_k(nT_s) \right),$$

where  $\Lambda((n-1)T_s) = w(0)$  for  $n = 1$ , and  $\Lambda((n-1)T_s) = w(0) + \sum_{j=1}^{n-1} \sum_{k \in \mathcal{V}_m} w_k(jT_s) + \sum_{j=1}^{n-1} \sum_{k \in \mathcal{V}_s} w_k(jT_s)$  for  $n = 2, 3, \dots$  which can be updated recursively over time. The final decision at the fusion center is then given by,

$$\delta_F(nT_s) = \begin{cases} 1 & \geq \\ \text{if } \Lambda(nT_s) & \rho(nT_s) \\ 0 & < \end{cases}, \quad (15)$$

where  $\rho(nT_s)$  is the threshold of the counting decision rule at the fusion center at time  $nT_s$ . The decision threshold  $\rho(nT_s)$  is selected such that the overall system false alarm probability at the fusion center is less than a desired level, say  $\alpha_2$ . Note that, for general non-identical BSCs,  $\Lambda(nT_s)$  is a sum of independent but non-identical binary random variables. Using the Lindeberg-Feller central limit theorem for independent random variables under certain regularity conditions (see Appendix D) [24], it can be shown that  $\Lambda(nT_s)$  is distributed under two hypotheses as,

$$\text{Under } \mathcal{H}_1 : \Lambda(nT_s) \sim \mathcal{N}(\mu_{\Lambda_1}, \sigma_{\Lambda_1}^2)$$

and

$$\text{Under } \mathcal{H}_0 : \Lambda(nT_s) \sim \mathcal{N}(\mu_{\Lambda_0}, \sigma_{\Lambda_0}^2).$$

where  $\mu_{\Lambda_1}(nT_s) = P_D^0 + \sum_{j=1}^n \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(jT_s) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(jT_s)$ ,  $\sigma_{\Lambda_1}^2(nT_s) = P_D^0(1 - P_D^0) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(jT_s)(1 - \mu_{d_k}^m(jT_s)) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(jT_s)(1 - \mu_{d_k}^s(jT_s))$ ,  $\mu_{\Lambda_0}(nT_s) = P_F^0 + \sum_{j=1}^n \sum_{k \in \mathcal{V}_m} \mu_{f_k}^m(jT_s) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_s} \mu_{f_k}^s(jT_s)$  and  $\sigma_{\Lambda_0}^2(nT_s) = P_F^0(1 - P_F^0) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_m} \mu_{f_k}^m(jT_s)(1 - \mu_{f_k}^m(jT_s)) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_s} \mu_{f_k}^s(jT_s)(1 - \mu_{f_k}^s(jT_s))$ . Then the detection probability at the fusion center can be shown to be

$$P_D(nT_s) = Pr(\Lambda(nT_s) \geq \rho(nT_s) | \mathcal{H}_1) = Q\left(\frac{\rho(nT_s) - \mu_{\Lambda_1}(nT_s)}{\sigma_{\Lambda_1}(nT_s)}\right), \quad (16)$$

where  $\rho(nT_s) = Q^{-1}(\alpha_2)\sigma_{\Lambda_0}(nT_s) + \mu_{\Lambda_0}(nT_s)$ .

### D. Mobility management for mobile nodes

In this section, we find the best movement schedule for each mobile node in order to maximize the detection probability at the fusion center within a desired delay constraint (or before the target disappeared). We assume that each mobile node moves with the same speed such that  $v_k = \bar{v}$  for  $k \in \mathcal{V}_m$ . Note that, each mobile node can move a distance of  $\bar{v}T_s$  during each time period of  $T_s$  in a direction selected from

the set  $\Theta = \{\theta^1, \theta^2, \dots, \theta^K\}$ . Let  $\mathcal{C}_k(nT_s)$  be the candidate locations of mobile node  $k$  at time  $nT_s$ . Note that, if there are no terrain constraints such that nodes can move heading to the possible target locations on straight line, a certain number of steps can be made along a straight line as time goes, and there is only one direction. The following discussion is applicable, if mobile nodes are not in a position to direct towards the possible target locations on a straight line from their original locations due environmental and terrain constraints. Denote  $T_D$  to be the desired delay constraint which is equal or less than the average time that the target remains active after appearing. The requirement is to maximize the detection probability at the fusion center,  $P_D(n_D T_s)$ , where  $n_D = \lfloor \frac{T_D}{T_s} \rfloor$ , with the best movement plan for each mobile node. Equivalently, we need to find the best direction that  $k$ -th mobile node should move at time  $jT_s$ , for  $k \in \mathcal{V}_m$  and  $j = 0, 1, 2, \dots, n_D$ , to obtain the maximum (over all possible movements) detection probability at time  $n_D T_s$ . Denote  $\hat{\Theta}_k = \{\hat{\theta}_k(T_s), \hat{\theta}_k(2T_s), \dots, \hat{\theta}_k(n_D T_s)\}$  be the best set of movement directions at each time step for node  $k$ . Now the problem can be formulated as,

$$\begin{aligned} & \text{Find the set } \{\hat{\Theta}_1, \hat{\Theta}_2, \dots, \hat{\Theta}_{N_m}\} \\ & \text{such that} \\ & P_D(n_D T_s) \text{ is maximized} \end{aligned} \quad (17)$$

If the fusion center were to compute the movement plan beforehand for each mobile node, in general, the optimization has to search over as many as  $N_m \times |\Theta| \times n_D$  variables leading to a search space of size  $2^{N_m |\Theta| n_D}$  where  $|\Theta|$  is the cardinality of the set  $\Theta$ . Although this brute-force approach will result in the optimal solution, it is computationally expensive. Thus, in the following we propose a near-optimal approach for each mobile node to select its best movement direction at each time step based on its own performance measure: i.e. each node moves in a direction at each time step which would lead to maximum individual performance at time  $n_D T_s$ .

Note that the detection probability at the fusion center at time  $nT_s$  is given by (16). The required optimization problem is to find optimal movement plan for each mobile node  $k$  for each  $j = 0, 1, 2, \dots, n_D$  such that  $P_D(n_D T_s)$  is maximized. Maximizing  $P_D(nT_s)$  in (16) is equivalent to minimizing the argument in the  $Q$ -function. Note that in the following analysis we assume  $P_D^0 = P_F^0 = 0$  for simplicity but the similar results will hold for general values of  $P_D^0$  and  $P_F^0$ . Denote  $f(\boldsymbol{\mu}_d)$  be the argument of the  $Q$ -function in (16) where,

$$f(\boldsymbol{\mu}_d(nT_s)) = \frac{\rho - \frac{1}{n} \boldsymbol{\mu}_d^T(nT_s) \mathbf{e}}{\sqrt{\frac{1}{n^2} \boldsymbol{\mu}_d^T(nT_s) \mathbf{e} - \frac{1}{n^2} \boldsymbol{\mu}_d^T(nT_s) \boldsymbol{\mu}_d(nT_s)}} \quad (18)$$

where  $\mathbf{e}$  is the  $Nn$ -length vector containing all ones,

$\boldsymbol{\mu}_d(nT_s) = [P_D^0, \mu_{d_1}^m(jT_s), \dots, \mu_{d_{N_m}}^m(jT_s), \mu_{d_1}^s(jT_s), \dots, \mu_{d_{N_s}}^s(jT_s), j = 1 \dots, n]^T$  is the  $Nn$ -length vec-

tor containing all the elements in the sum  $\mu_{\Lambda_1}(nT_s)$  so that  $\mu_{\Lambda_1}(nT_s) = \frac{1}{n}\boldsymbol{\mu}_d^T(nT_s)\mathbf{e}$ . Then as given by [20], since  $P_D^0, \mu_{d_k}^m(jT_s), \mu_{d_l}^s(jT_s) \in (0, 1)$  for  $k \in \mathcal{V}_m, l \in \mathcal{V}_s$  and  $j = 1 \dots, n$ , using the first order Taylor series expansion around central point,  $f(\boldsymbol{\mu}_d(nT_s))$  can be approximated as,

$$f(\boldsymbol{\mu}_d(nT_s)) \approx -\frac{2}{\sqrt{Nn}}\mu_{\Lambda_1}(nT_s) + \frac{2\rho\sqrt{n}}{\sqrt{N}} + H \quad (19)$$

where  $H$  denotes the second and higher order terms in the Taylor series expansion. It is seen from (19) that if  $H$  and the sum  $\mu_{\Lambda_1}(n_D T_s) = \left[ \frac{1}{n} \sum_{j=1}^{n_D} \left( \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(jT_s) + \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(jT_s) \right) \right]$  were to be independent of each other, then  $f(\boldsymbol{\mu}_d(nT_s))$  will be monotonically decreasing with increasing  $\mu_{\Lambda_1}(nT_s)$ . It was shown in [20] that, with high probability,  $f(\boldsymbol{\mu}_d(nT_s))$  is indeed decreasing when the sum  $\mu_{\Lambda_1}(nT_s)$  is increasing. Thus, with high probability, maximizing the detection probability at the fusion center at time  $nT_s$  is equivalent to maximizing the sum  $\mu_{\Lambda_1}(nT_s)$ . Since each mobile and static node performs their detection problems independent of each other, maximizing  $\sum_{j=1}^{n_D} \mu_{d_k}^m(jT_s)$  over all possible movement plans for  $k \in \mathcal{V}_m$  will maximize the sum  $\mu_{\Lambda_1}(nT_s)$  at time  $nT_s$ .

Note that  $\sum_{j=1}^{n_D} \mu_{d_k}^m(jT_s)$  for the  $k$ -th mobile node is given by

$$\begin{aligned} \sum_{j=1}^{n_D} \mu_{d_k}^m(jT_s) &= \sum_{j=1}^{n_D} (\bar{P}_{d_k}^m(jT_s)(1 - p_k) + (1 - \bar{P}_{d_k}^m(jT_s))p_k) \\ &= p_k + (1 - 2p_k) \sum_{j=1}^{n_D} \bar{P}_{d_k}^m(jT_s). \end{aligned} \quad (20)$$

Hence maximizing  $\sum_{j=1}^{n_D} \mu_{d_k}^m(jT_s)$  at  $k$ -th mobile node is equivalent to maximizing  $\sum_{j=1}^{n_D} \bar{P}_{d_k}^m(jT_s)$  where  $\bar{P}_{d_k}^m(jT_s)$  is given by (10).

Now the optimization problem is equivalent to finding the optimal set  $\hat{\Theta}_k \equiv \{\hat{\theta}_k(T_s), \hat{\theta}_k(2T_s), \dots, \hat{\theta}_k(n_D T_s)\}$  which maximizes the sum of detection probabilities up to time  $n_D T_s$  at the  $k$ -th mobile node as given in (10). Denote  $\bar{P}_{d_k}^m(0, n_D) = \sum_{j=1}^{n_D} \bar{P}_{d_k}^m(jT_s)$  to be the sum of detection probabilities at  $k$ -th mobile node up to time  $n_D T_s$  where  $\bar{P}_{d_k}^m(jT_s)$  as given by (10) is the detection probability related to the decision made by  $k$ -th mobile node based on observations during time interval  $((j-1)T_s, jT_s)$ . In the following, we convert the required problem into an time expansion graph, such that the required problem becomes a shortest path problem and the solution for the optimization problem can be obtained, for example via forward dynamic programming.

Let  $\Theta(jT_s) = \{\theta^1(jT_s), \theta^2(jT_s), \dots, \theta^K(jT_s)\}$  be the state space at time (stage)  $jT_s$  for the  $k$ -th mobile node which represents the set of directions that the  $k$ -th mobile node can move at time  $jT_s$ . We assume that each mobile node has the same candidate set of directions that it can move at a given time step (However this assumption can be generalized to have different candidate sets for different mobile nodes).

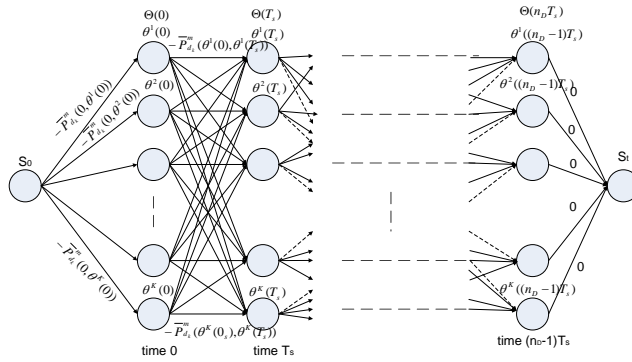


Fig. 4. Shortest path representation for finding maximum detection probability at time  $n_D T_s$  at  $k$ -th mobile node

For clarity, let us write the sum of detection probabilities  $\bar{P}_{d_k}^m(0, n_D)$  as,

$$\bar{P}_{d_k}^m(0, n_D) = \sum_{j=1}^{n_D} \bar{P}_{d_k}^m((j-1)T_s, jT_s), \quad (21)$$

where  $\bar{P}_{d_k}^m((j-1)T_s, jT_s)$  is the average detection probability corresponding to the decision made based on the observations during the interval  $((j-1)T_s, jT_s)$  which is given by (10). Now we construct a trellis as shown in Fig. 4 where the states of the trellis at time (stage)  $jT_s$  represents the directions (states) from the finite set  $\Theta(jT_s)$ . In Fig. 4, the trellis diagram is preceded by  $s_0$  and followed by  $s_t$  which are two dummy nodes. Denote  $\bar{P}_{d_k}^m(\theta^p(j-1), \theta^q(j))$  represents the detection probability for the decision based on observations collected during transition from state  $\theta^p(j-1) \in \Theta((j-1)T_s)$  to  $\theta^q(j) \in \Theta(jT_s)$ . This represents the detection probability for the decision based on the observations collected during the time interval  $(jT_s, (j+1)T_s)$  when the  $k$ -th mobile node selects the direction  $\theta^q(j)$  at time instant  $jT_s$  given that the direction selected at time  $(j-1)T_s$  is  $\theta^p(j-1)$ . Now, branch from  $s_0$  to  $\theta^p(0) \in \Theta(0)$  is assigned the metric  $-\bar{P}_{d_k}^m(0, \theta^p(0))$  where  $\bar{P}_{d_k}^m(0, \theta^p(0))$  represents the average detection probability for the decision based on observations collected by the  $k$ -th mobile node if it selects the direction  $\theta^p(0)$  from its original location. Branch from state  $\theta^p(j-1) \in \Theta((j-1)T_s)$  to  $\theta^q(j) \in \Theta(jT_s)$  is assigned the metric  $-\bar{P}_{d_k}^m(\theta^p(j-1), \theta^q(j))$  for  $j = 1, 2, \dots, n_D - 1$ . Then finding maximum value of the sum  $\bar{P}_{d_k}^m(0, n_D) = \sum_{j=1}^{n_D} \bar{P}_{d_k}^m((j-1)T_s, jT_s)$  from time 0 to time  $n_D T_s$  over all possible directions is equivalent to finding the shortest path between the node  $s_0$  to  $s_t$  as in the graph shown in Fig. 4, and the optimal  $\hat{\Theta}_k$  is the set of states in the shortest path. Note that this shortest path can be computed by forward dynamic programming with average complexity of order  $O(n_D |\Theta|^2)$  per mobile node.

In solving the shortest path algorithm via dynamic programming for the original optimization problem in (17), the movement plan for each mobile node needs to be computed beforehand at time  $t = 0$  which also requires the knowledge of the candidate set of locations at each time. In the following we show that a sequential approach where the  $k$ -th mobile node determines its movement direction at time  $jT_s$  based

on only its current information and expected information at time  $(j + 1)T_s$  yields closer performance compared to that with dynamic programming approach under certain conditions.

We consider the following approach where mobile nodes select best direction to move at time  $jT_s$  sequentially. The idea is to select the best location for the  $k$ -th mobile node at time step  $jT_s$  such that the observations collected during time interval  $[jT_s, (j + 1)T_s]$  would lead to best detection performance over all possible directions. According to the signal model (2), when a mobile node is getting closer to the target, the SNR at the node is increased, subsequently increasing the detection probability at the  $k$ -th mobile node. Hence, the direction at time  $t = jT_s$  is chosen as in the following:

$$\begin{aligned} \theta_k(jT_s) &= \operatorname{argmax}_{\theta_i \in \Theta} \{\bar{P}_{d_k}^m((j + 1)T_s, \theta_i)\}, \\ \text{for } j &= 0, 1, 2, \dots, n_D, \end{aligned} \tag{22}$$

where  $\bar{P}_{d_k}^m((j + 1)T_s, \theta_i)$  is the average detection probability at the  $k$ -th mobile node at time step  $(j + 1)T_s$  if the direction  $\theta_i \in \Theta$  is selected at time  $jT_s$ ,  $n_D$  is the step index at which  $P_D(n_D T_s) \geq \xi_D$  for the first time. The average detection probability at  $k$ -th mobile node at time  $jT_s$  is as given by (10). From the simulation results, we see that, when the candidate set of directions that any mobile node can move at a given time is the same, and a node moves at the same speed in all directions, the performance of this scheme coincides with the near-optimal scheme which is computed based on shortest path algorithm.

## V. DETECTION PERFORMANCE WITH DECISION FUSION ARCHITECTURE 2: NODES UPDATING DECISIONS OVER TIME

In this section, develop an alternate formulation for decision fusion in the hybrid sensor network when the nodes are updating decisions over time, where the impact of the node mobility is taken into account at the node level decisions. As in Section IV, let  $P_D^0$  and  $P_F^0$  be the overall (system) detection and false alarm probabilities at time  $t = 0$ . If  $P_D^0 \geq \epsilon_1$  and  $P_F^0 \leq \epsilon_2$ , for particular  $\epsilon_1$  and  $\epsilon_2$ , we say that a target is detected at time zero with a lower confidence level. After a target is detected with a lower confidence level, mobile and static nodes perform the following hypothesis testing problem, at time  $t = nT_s$ , based on the observations collected until time  $nT_s$ :

$$\begin{aligned} \mathcal{H}_1 &: z_k(t) = m_k(t) + u_k(t); \quad 0 \leq t \leq nT_s, \\ \mathcal{H}_0 &: z_k(t) = u_k(t); \quad 0 \leq t \leq nT_s. \end{aligned} \tag{23}$$

Note that in this section we consider that each node performs hypothesis testing (23) based on the observations collected during the interval  $[0, nT_s]$ , contrast to Section IV. The decision fusion architecture in this case is shown in Fig. 5. As shown in Fig. 5, at each time instant  $nT_s$ , each distributed node performs

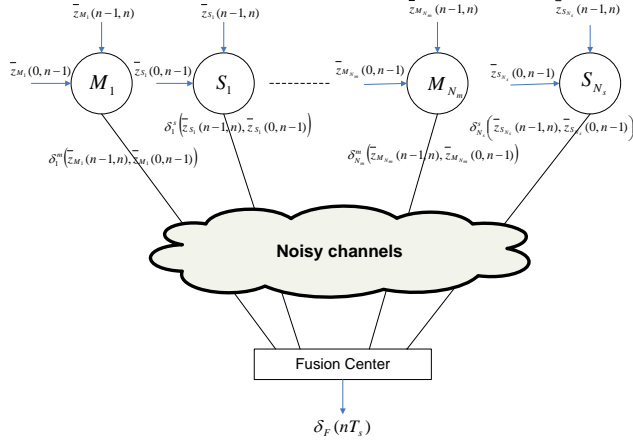


Fig. 5. Decision Fusion Architecture for the Hybrid Sensor Network with Nodes Updating Decisions over Time

a local detection based on the observations collected at the current time interval  $(n-1)T_s \leq t < nT_s$  and previous observations up to time  $(n-1)T_s$  which can be computed recursively for  $n = 1, 2, \dots$ . These local decisions are transmitted to the fusion center over a noisy communication channel at each time step  $t = nT_s$ . The fusion center combines these noise corrupted decisions and the initial decision at time  $t = 0$  to reach at a final decision on whether the target is present or absent.

#### A. Detection performance at $k$ -th mobile node

Similar to Section IV, we assume that each node performs  $\alpha_1$ -level N-P detector to decide whether the target is present or absent based on the observations collected during time interval  $(0, nT_s]$ . The decision statistic and the threshold for the N-P detector corresponding to (8) now can be shown as,

$$\delta_k^m(nT_s) = \begin{cases} 1 & \geq \\ \text{if } \bar{z}_k(0, n) & \tau_k^m(n) \\ 0 & < \end{cases}, \quad (24)$$

where  $\bar{z}_k(0, n) = \int_0^{nT_s} z_k \overline{m_k(t)} dt = \bar{z}_k(0, n-1) + \int_{(n-1)T_s}^{nT_s} z_k \overline{m_k(t)} dt$  is the decision statistic which can be computed recursively at each time step and  $\tau_k^m(n) = \sigma_u^2 \eta_k^m(n) + \frac{1}{2} \bar{E}_k^m(0, n)$  is the corresponding threshold, for  $k \in \mathcal{V}_m$  where  $\bar{E}_k^m(0, n) = \mathbb{E}_{x_0, y_0} \{E_k^m(0, n)\}$  as defined in subsection IV-A.

*Proposition 3:* With decision fusion model 2, for  $\alpha_1$ -level N-P test, the threshold and the detection probability at the  $k$ -th mobile node, at time  $nT_s$  are given by ,

$$\tau_k^m(n) = \sigma_u Q^{-1}(\alpha_1) \sqrt{E_k^m(0, n)} \quad (25)$$

and

$$P_{d_k}^m(nT_s) = \mathbb{E}_{x_0, y_0} \left\{ Q \left( Q^{-1}(\alpha_1) - \frac{\tilde{E}_k(x_0, y_0; 0, n)}{\sigma_u \sqrt{E_k^m(0, n)}} \right) \right\}. \quad (26)$$



$$E_k^m(0, n) = \sum_{j=1}^n \frac{2A_0^2}{\sqrt{\Delta_k(j-1)}} \arctan \left( \frac{2a_k T_s \sqrt{\Delta_k(j-1)}}{\Delta_k(j-1) + b_k(j-1)(b_k(j-1) + 2a_k T_s)} \right) \quad (28)$$

Note that  $E_k^m(0, n)$  at the  $k$ -th mobile node is  $E_k^m(0, n) = \sum_{j=1}^n \int_{(j-1)T_s}^{jT_s} m_k^2(t) dt$  which is essentially the instant total signal energy received during the period  $0 \leq t \leq nT_s$ , for a given target location. Then we have,

$$\begin{aligned} E_k^m(j-1, j) &= \int_{(j-1)T_s}^{jT_s} m_k^2(t) dt = \int_{(j-1)T_s}^{jT_s} \frac{A_0^2}{r_k^2(t)} dt \\ &= \int_{(j-1)T_s}^{jT_s} A_0^2 \left( (x'_k(j-1) + v_k(t - (j-1)T_s) \cos \theta_k(jT_s))^2 \right. \\ &\quad \left. + (y'_k(j-1) + v_k(t - (j-1)T_s) \sin \theta_k(jT_s))^2 \right)^{-1} dt \\ &= \frac{2A_0^2}{\sqrt{\Delta_k(j-1)}} \arctan \left( \frac{2a_k T_s \sqrt{\Delta_k(j-1)}}{\Delta_k(j-1) + b_k(j-1)(b_k(j-1) + 2a_k T_s)} \right) \end{aligned} \quad (27)$$

where  $x'_k(j-1) = x_k((j-1)T_s) - x_0$ ,  $y'_k(j-1) = y_k((j-1)T_s) - y_0$ ,  $a_k = v_k^2$ ,  $b_k(j-1) = 2v_k(x'_k(j-1) \cos \theta_k(jT_s) + y'_k(j-1) \sin \theta_k(jT_s))$ ,  $c_k(j-1) = x_k'^2(j-1) + y_k'^2(j-1)$  and  $\Delta_k(j-1) = 4a_k c_k(j-1) - b_k^2(j-1)$ . Note that (27) holds only if  $\Delta_k(j-1) > 0$  which is shown to be true in the following.

$$\begin{aligned} \Delta_k(j-1) &= 4v_k^2(x_k'^2(j-1) + y_k'^2(j-1)) \\ &\quad - 4v_k^2(x'_k(j-1) \cos \theta_k(jT_s) + y'_k(j-1) \sin \theta_k(jT_s))^2 \\ &= 4v_k^2(x'_k(j-1) \sin \theta_k(jT_s) - y'_k(j-1) \cos \theta_k(jT_s))^2 \\ &> 0. \end{aligned}$$

Then  $E_k^m(0, n)$  is given by (28).

### B. Detection performance at the $k$ -th static node

Similarly, for the  $k$ -th static node, the  $\alpha_1$ -level N-P threshold and the detection probability at time  $nT_s$  are given by the following proposition.

*Proposition 4:* For static nodes, the optimal threshold and the detection probability for the  $\alpha_1$ -level NP test are given by,

$$\tau_k^s(n) = \sigma_u Q^{-1}(\alpha_1) \bar{m}_k \sqrt{nT_s} \quad (29)$$

and

$$P_{d_k}^s(nT_s) = \mathbb{E}_{x_0, y_0} \left\{ Q \left( Q^{-1}(\alpha_1) - \frac{m_k(x_0, y_0) \sqrt{nT_s}}{\sigma_u} \right) \right\}. \quad (30)$$

### C. Decision fusion performance with noisy communication

Similar to subsection IV-C, we evaluate the decision fusion performance at the fusion center at time  $nT_s$  with BSC channels. Now, since the effect of the mobility is taken at the node level, the decision statistic at the fusion center is taken as,  $\tilde{\Lambda}(nT_s)$ , where

$$\tilde{\Lambda}(nT_s) = w(0) + \sum_{k \in \mathcal{V}_m} w_k(nT_s) + \sum_{k \in \mathcal{V}_s} w_k(nT_s),$$

where  $w(0) = 1$  with probability  $P_D^0$  and  $w(0) = 0$  with probability  $1 - P_D^0$  under  $\mathcal{H}_1$  and  $w(0) = 1$  with probability  $P_F^0$  and  $w(0) = 0$  with probability  $1 - P_F^0$  under  $\mathcal{H}_0$  as in section IV-C.  $w_k(nT_s)$  for  $n = 1, \dots$  is same as given by (13) and (14) under two hypotheses where now  $\mu_{d_k}^m(nT_s) = P_{d_k}^m(nT_s)(1 - p_k) + (1 - P_{d_k}^m(nT_s))p_k$ ,  $\mu_{d_k}^s(nT_s) = P_{d_k}^s(nT_s)(1 - p_k) + (1 - P_{d_k}^s(nT_s))p_k$ ,  $\mu_{f_k}^m(nT_s) = \alpha_1(1 - p_k) + (1 - \alpha_1)p_k$  and  $\mu_{f_k}^s(nT_s) = \alpha_1(1 - p_k) + (1 - \alpha_1)p_k$  with  $P_{d_k}^m(nT_s)$  and  $P_{d_k}^s(nT_s)$  are given by (26) and (30), respectively. The detection probability corresponding to the decision rule based on majority rule is given by (following a similar approach as in subsection IV-C),

$$P_D(nT_s) = Pr(\tilde{\Lambda}(nT_s) \geq \tilde{\rho}(nT_s) | H_1) = Q\left(\frac{\tilde{\rho}(nT_s) - \mu_{\tilde{\Lambda}_1}(nT_s)}{\sigma_{\tilde{\Lambda}_1}(nT_s)}\right), \quad (31)$$

where  $\mu_{\tilde{\Lambda}_1}(nT_s) = P_D^0 + \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(nT_s) + \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(nT_s)$  and  $\sigma_{\tilde{\Lambda}_1}^2(nT_s) = P_D^0(1 - P_D^0) + \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(nT_s)(1 - \mu_{d_k}^m(nT_s)) + \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(nT_s)(1 - \mu_{d_k}^s(nT_s))$  and  $\tilde{\rho}(nT_s) = Q^{-1}(\alpha_2)\sigma_{\tilde{\Lambda}_0} + \mu_{\tilde{\Lambda}_0}$  is the threshold of the detector which ensures that the false alarm probability is less than or equal to  $\alpha_2$ , and  $\mu_{\tilde{\Lambda}_0}(nT_s) = P_F^0 + \sum_{k \in \mathcal{V}_m} \mu_{f_k}^m(nT_s) + \sum_{k \in \mathcal{V}_s} \mu_{f_k}^s(nT_s)$  and  $\sigma_{\tilde{\Lambda}_0}^2(nT_s) = P_F^0(1 - P_F^0) + \sum_{k \in \mathcal{V}_m} \mu_{f_k}^m(nT_s)(1 - \mu_{f_k}^m(nT_s)) + \sum_{k \in \mathcal{V}_s} \mu_{f_k}^s(nT_s)(1 - \mu_{f_k}^s(nT_s))$ .

### D. Mobility management for mobile nodes

Similar to the scenario in Section IV, we need to find the best movement schedule for each mobile node in order to maximize the detection probability at the fusion center within a desired delay constraint or before the target disappears. The idea is to find the optimal movement schedule for each mobile node  $k$  such that the detection probability at the fusion center within a desired delay constraint, is maximized. As in subsection IV-D, denote  $T_D$  to be the desired delay constraint and  $\hat{\Theta}_k = \{\hat{\theta}_k(T_s), \hat{\theta}_k(2T_s), \dots, \hat{\theta}_k(n_D T_s)\}$  be the optimal set of movement directions at each time step for node  $k$ . following a similar approach as in subsection IV-D, it can be shown that with high probability, maximizing the detection probability at the fusion center at time  $nT_s$  (31) is equivalent to maximizing the sum  $\mu_{\Lambda_1}(nT_s) = \sum_{k \in \mathcal{V}_m} \mu_{d_k}^m(nT_s) + \sum_{k \in \mathcal{V}_s} \mu_{d_k}^s(nT_s)$ . Since mobile and static nodes perform their detection problems independent of each other, maximizing each  $\mu_{d_k}^m(nT_s)$  for  $k \in \mathcal{V}_m$  over all possible movement plans will maximize the sum  $\mu_{\Lambda_1}(nT_s)$  at time  $nT_s$ . Similar to subsection IV-D, it can be shown that maximizing  $\mu_{d_k}^m(nT_s)$  at  $k$ -th mobile node is equivalent to maximizing  $P_{d_k}^m(nT_s)$  at the  $k$ -th mobile node, given by (26).

Note that if the exact target location is known, then maximizing (26) at the  $k$ -th mobile node is equivalent to maximizing the total energy collected during the interval  $(0, n]$ ,  $E_k^m(0, n)$  as given in (28). Then the approach given in subsection IV-D, can be directly used to find the optimal movement directions at each time step, where now the metrics of branches of the trellis in Fig. 4 are replaced by  $-E_k^m(\theta^p(j-1), \theta^q(j))$  which represents the energy collected during transition from state  $\theta^p(j-1) \in \Theta((j-1)T_s)$  to  $\theta^q(j) \in \Theta(jT_s)$ .

## VI. MINIMUM SET OF MOBILE NODES

Since allowing nodes to be mobile is expensive in terms of energy, it is important to determine the minimum number of mobile nodes (from the set  $\mathcal{V}_m$ ) that should be directed to move to achieve a certain detection probability within a given delay constraint or before the target disappears. In the following, we consider the problem of finding the smallest set of mobile nodes in order to maintain the maximum detection probability achieved by time  $T_D$  is greater than some threshold value. For the discussion given below, we assume the case where exact target location is known with the decision fusion model as given by Section V in which nodes are updating decisions over time.

Let the required detection probability threshold at time  $T_D$  be  $\xi_D$ . The problem is to find the minimum set of mobile nodes, that should be used in the network to reach a desired performance level within a desired delay constraint. Formally, we can write the optimization problem as,

$$\begin{aligned} & \min |\mathcal{S}_m| \\ & \text{such that } \mathcal{S}_m \subset \mathcal{V}_m \\ & \text{and } P_D(n_D T_s) \geq \xi_D \end{aligned} \quad (32)$$

where, as before,  $n_D = \lfloor \frac{T_D}{T_s} \rfloor$ . Assuming that  $\xi_D \geq \frac{1}{2}$ , the inequality (32) can be further simplified as given below (For simplicity, we assume perfect communication channels such that  $p_k = 0$  for all  $k \in \mathcal{V}$ ):

$$\begin{aligned} & P_D(n_D T_s) \geq \xi_D \\ \equiv & Q\left(\frac{\tilde{\rho}(n_D T_s) - \mu_{\tilde{\Lambda}_1}(n_D T_s)}{\sigma_{\tilde{\Lambda}_1}(n_D T_s)}\right) \geq \xi_D \end{aligned} \quad (33)$$

$$\equiv \frac{\tilde{\rho}(n_D T_s) - \mu_{\tilde{\Lambda}_1}(n_D T_s)}{\sigma_{\tilde{\Lambda}_1}(n_D T_s)} \leq \beta \quad (34)$$

$$\Rightarrow \tilde{\rho}(n_D T_s) - \mu_{\tilde{\Lambda}_1}(n_D T_s) \leq \beta \sigma_{\tilde{\Lambda}_1}(n_D T_s) \quad (35)$$

$$\Rightarrow (\tilde{\rho}(n_D T_s) - \mu_{\tilde{\Lambda}_1}(n_D T_s))^2 \geq \beta^2 \sigma_{\tilde{\Lambda}_1}^2(n_D T_s) \quad (36)$$

where  $\mu_{\tilde{\Lambda}_1}(n_D T_s) = \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s) + \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s)$  and  $\sigma_{\tilde{\Lambda}_1}^2(n_D T_s) = \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s)(1 - P_{d_k}^m(n_D T_s)) + \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s)(1 - P_{d_k}^s(n_D T_s))$  and  $\beta = Q^{-1}(\xi_D)$ . Note that here  $P_{d_k}^m(n_D T_s)$  and  $P_{d_k}^s(n_D T_s)$  are given

$$\begin{aligned}
& - (2\tilde{\rho} + \beta^2) \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s) + \left( \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s) \right)^2 + \beta^2 \sum_{k \in \mathcal{S}_m} P_{d_k}^{m2}(n_D T_s) + 2 \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s) \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s) \\
& \geq (2\tilde{\rho} + \beta^2) \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s) - \beta^2 \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^{s2}(n_D T_s) - \left( \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s) \right)^2 - \tilde{\rho}^2
\end{aligned} \tag{38}$$

by (26) and (30) without the outer expectation with respect to target locations (since we assume exact target locations for this analysis). Note that hereafter we use  $\tilde{\rho}(n_D T_s)$  and  $\tilde{\rho}$  interchangeably when there is no ambiguity. Since mobile nodes which are not moving also make observations at their stationary configuration, we will have the set of static nodes as  $\mathcal{V} \setminus \mathcal{S}_m$  when the set of mobile nodes is  $\mathcal{S}_m$ . Note that (35) is obtained from (34) since  $\sigma_{\tilde{\lambda}_1}(n_D T_s) > 0$ . If we constrain  $\xi_D \geq \frac{1}{2}$  which is a reasonable assumption, the argument of the Q- function in (33) should be negative. Also since  $\sigma_{\tilde{\lambda}_1}(n_D T_s) > 0$  for  $n_D = 1, 2, \dots$ , to satisfy  $Q\left(\frac{\tilde{\rho} - \mu_{\tilde{\lambda}_1}(n_D T_s)}{\sigma_{\tilde{\lambda}_1}(n_D T_s)}\right) \geq \xi_D \geq \frac{1}{2}$ , the following condition should hold:  $\tilde{\rho}(n_D T_s) - \mu_{\tilde{\lambda}_1}(n_D T_s) < 0$ . Note that,

$$\begin{aligned}
\tilde{\rho}(n_D T_s) - \mu_{\tilde{\lambda}_1}(n_D T_s) & = Q^{-1}(\alpha_2) \sqrt{P_F^0(1 - P_F^0) + N\alpha_1(1 - \alpha_1)} \\
& - (P_D^0 + \sum_{k \in \mathcal{S}_m} P_{d_k}^m(n_D T_s) + \sum_{k \in \mathcal{V} \setminus \mathcal{S}_m} P_{d_k}^s(n_D T_s))
\end{aligned} \tag{37}$$

To make sure the condition  $\tilde{\rho}(n_D T_s) - \mu_{\tilde{\lambda}_1}(n_D T_s) < 0$  is satisfied, from (37), it can be seen that  $\sum_{k=1}^N P_{d_k}^m(n_D T_s) \geq Q^{-1}(\alpha_2) \sqrt{P_F^0(1 - P_F^0) + N\alpha_1(1 - \alpha_1)} - P_D^0 = C_0$  at the worst case. This says that if  $\sum_{k=1}^N P_{d_k}^m(n_D T_s) < C_0$  for some  $n_D$  and  $\xi_D \geq \frac{1}{2}$ , the required performance can not be achieved during the required time delay even if all nodes are mobile such that  $\mathcal{S}_m \equiv \mathcal{V}$ . In the following we consider only the case where  $\sum_{k=1}^N P_{d_k}^m(n_D T_s) \geq C_0$  ensuring  $\tilde{\rho}(n_D T_s) - \mu_{\tilde{\lambda}_1}(n_D T_s) < 0$ . Thus (36) is obtained from (35). The inequality (36) can be further simplified as in (38). The problem is to find the minimum size set  $\mathcal{S}_m$  such that, inequality (38) is satisfied. To find this, in general we need to search over a maximum of  $2^{N_m}$  possibilities.

In the following we will show how to obtain the solution with reduced complexity under certain conditions. Note that as discussed in subsection V-D, the maximum  $P_{d_k}^m(n_D T_s)$  for each  $k \in \mathcal{V}_m$  at time  $n_D T_s$  can be computed. Without loss of generality, let us arrange  $P_{d_k}^m(n_D T_s)$ 's in descending order for  $k \in \mathcal{V}_m$  such that  $P_{d_1}^m(n_D T_s) \geq P_{d_2}^m(n_D T_s) \geq \dots \geq P_{d_{N_m}}^m(n_D T_s)$ . Then the set denoted by  $\mathcal{S}_m^k$  consists of the indices of first  $k$  mobile nodes. Now define two functions  $f_1(k)$  and  $f_2(k)$  such that,

$$f_1(k) = (2\tilde{\rho} + \beta^2) \sum_{j=1}^k P_{d_j}^m(n_D T_s) \tag{39}$$

and

$$\begin{aligned}
f_2(k) &= \left( \sum_{j=1}^k P_{d_j}^m(n_D T_s) \right)^2 + \beta^2 \sum_{j=1}^k P_{d_j}^{m2}(n_D T_s) \\
&+ 2 \sum_{j=1}^k P_{d_j}^m(n_D T_s) \sum_{j \in \mathcal{V} \setminus \mathcal{S}_m^k} P_{d_j}^s(n_D T_s)
\end{aligned} \tag{40}$$

for  $k = 0, 1, 2, \dots, N_m$  with  $f_1(0) = f_2(0) = 0$ .

Denote  $\mathcal{V}_s^k = \mathcal{V} \setminus \mathcal{S}_m^k$  to be the set containing all static node indices and the mobile node indices from  $k + 1$  to  $N_m$ , for  $k = 1, \dots, N_m$ . Clearly,  $\mathcal{V}_s^0 = \mathcal{V}$  and  $\mathcal{V}_s^{N_m} = \mathcal{V}_s$ . Define  $K_s(n_D, k)$  to be,

$$\begin{aligned}
K_s(n_D, k) &= (2\tilde{\rho} + \beta^2) \sum_{j \in \mathcal{V}_s^k} P_{d_j}^s(n_D T_s) - \beta^2 \sum_{j \in \mathcal{V}_s^k} P_{d_j}^{s2}(n_D T_s) \\
&- \left( \sum_{j \in \mathcal{V}_s^k} P_{d_j}^s(n_D T_s) \right)^2 - \tilde{\rho}^2.
\end{aligned} \tag{41}$$

*Theorem 1:* If  $P_{d_k}^m(n_D T_s)$ 's are arranged in descending order and  $f_1(k)$ ,  $f_2(k)$  and  $K_s(n_D, k)$  are defined as in (39), (40) and (41), respectively, then we can find a unique  $K_0$  such that,

$$f_2(k) - f_1(k) \geq K_s(n_D, k), \text{ for } k \geq K_0 \tag{42}$$

and

$$f_2(k) - f_1(k) < K_s(n_D, k), \text{ for } k < K_0. \tag{43}$$

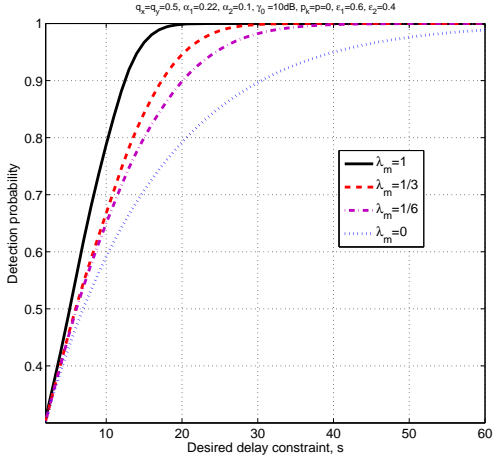
Then  $K_0$  is the minimum number of mobile nodes that should be used to meet the desired criteria where the minimum set  $\mathcal{S}_m^{K_0} = \{1, 2, \dots, K_0\}$ .

*Proof:* See Appendix C. ■

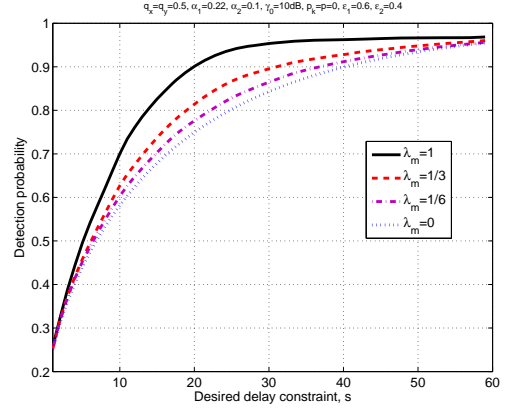
## VII. PERFORMANCE RESULTS

In this section, we evaluate the performance of the proposed target detection schemes using a hybrid sensor network. We assume there is a total of 30 sensors deployed in a square region of area  $100 \times 100m^2$  where the center is at  $(0, 0)$ . We assume that mobile node speed is constant for all directions and the same for all nodes. The time step  $T_s = 1s$  and each mobile node's speed is  $\bar{v} = 1m/s$ . We define the nominal SNR at each node to be  $\gamma_0 = A_0^2/\sigma_u^2$ . We also assume that the communication between nodes and the fusion center is over i.i.d. BSC's such that  $p_k = p$  for all  $k \in \mathcal{V}$ . At each time step, we assume that a mobile node can move a distance of  $\bar{v}T_s$  in directions corresponding to due-east, north-east, due-north, north-west, due-west, south-west, due-south and south-east or remain at the current location.  $X$  and  $Y$  coordinates of the target location are assumed to be binary with the following distribution:

$$x_0 = \begin{cases} x_a & \text{with } q_x \\ x_b & \text{with } 1 - q_x \end{cases} \tag{44}$$



(a)



(b)

Fig. 6. Detection Probability at the fusion center with desired detection delay under perfect communication:  $T_s = 1$  s,  $\bar{v} = 1$  m/s,  $\gamma_0 = 10$  dB,  $p = 0$ ,  $q_x = q_y = 0.5$ ,  $\alpha_1 = 0.22$ ,  $\alpha_2 = 0.1$ ,  $\epsilon_1 = 0.6$ ,  $\epsilon_2 = 0.4$  (a). with decision fusion model 1, (b). with decision fusion model 2

and

$$y_0 = \begin{cases} y_a & \text{with } q_y \\ y_b & \text{with } 1 - q_y \end{cases} \quad (45)$$

This type of target location model is justifiable in situations when there is a finite number of possible surveillance locations that the target can appear probabilistically, based on the prior knowledge or new information received after initial deployment. Note that with this target location model,  $\overline{m_k(t)}$  is given by,

$$\begin{aligned} \overline{m_k(t)} = & \frac{A_0}{\sqrt{(x_k(t) - x_a)^2 + (y_k(t) - y_a)^2}} q_x q_y + \frac{A_0}{\sqrt{(x_k(t) - x_a)^2 + (y_k(t) - y_b)^2}} q_x (1 - q_y) \\ & + \frac{A_0}{\sqrt{(x_k(t) - x_b)^2 + (y_k(t) - y_a)^2}} (1 - q_x) q_y + \frac{A_0}{\sqrt{(x_k(t) - x_b)^2 + (y_k(t) - y_b)^2}} (1 - q_x) (1 - q_y) \end{aligned} \quad (46)$$

In Fig.6, the time varying detection performance is shown with the node mobility algorithms presented in the paper. In following figures we assume that mobile nodes perform sequential node mobility management as discussed in sections IV-D and V-D since it can be seen that the performance with mobility algorithm based on sequential approach is much closer to that with evaluated based on forward dynamic programming algorithm (see Fig. 10 for comparison). In Fig. 6, we have let  $\gamma_0 = 10$  dB, f.a.p. (false alarm probability) at local nodes  $\alpha_1 = 0.22$ , f.a.p. at the fusion center  $\alpha_2 = 0.1$ , initial detection and false alarm probabilities  $\epsilon_1 = 0.6$ ,  $\epsilon_2 = 0.4$ ,  $q_x = q_y = 0.5$ , and  $x_a = -25$ ,  $x_b = 25$ ,  $y_a = -25$ ,  $y_b = 25$ . The detection performance is shown when the fraction of mobile nodes is varying for  $p = 0$ . Fig. 6(a) corresponds to the decision fusion architecture 1 (Section IV) while Fig. 6(b) corresponds to decision fusion model 2 in Section V. It can be seen from Fig. 6 that with scheme 1, adding a small number of nodes boosts the detection

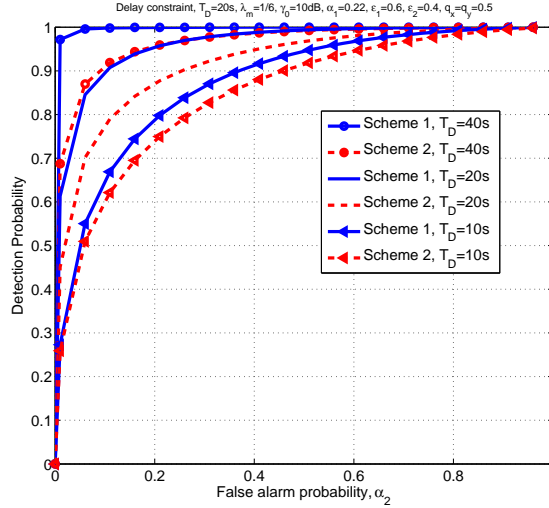


Fig. 7. ROC curves for two decision fusion models when the delay constraint is 20s:  $T_s = 1s$ ,  $\bar{v} = 1m/s$ ,  $\gamma_0 = 10dB$ ,  $p = 0$ ,  $q_x = q_y = 0.5$ ,  $\alpha_1 = 0.22$ ,  $\lambda_m = 1/6$ ,  $\epsilon_1 = 0.6$ ,  $\epsilon_2 = 0.4$

performance significantly compared to the performance with all static network. With the scheme 1, as time goes, since mobile nodes getting closer to possible target locations, according to the given probability distribution for target locations, a mobile node can make a binary decision based on the information collected at current time interval with a higher confidence level, when compared to a stationary sensor. On the other hand, stationary sensors make binary decisions based on its observations collected during current time interval, and the quality of these decisions remains the same over time since nodes are stationary. Then, according to the decision fusion model 1 described in Section IV, fusion center receives binary decisions over the time with higher confidence level when there are mobile sensors, resulting an improved performance compared to a all-stationary network.

As can be seen in Fig. 6(b), with decision fusion model 2, in which the nodes update decisions over time, the performance is improved significantly by adding a relatively large number of nodes compared to that with the model 1 under same network conditions. According to the decision fusion model 2, static nodes also collect energy over the time and decisions are getting more accurate as the time goes. For moderate and higher nominal SNR values, a static node may collect sufficient energy at its stationary locations compared to that is collected by a mobile node while moving towards possible target locations, since for large and moderate  $\gamma_0$ , even sensors located far away from the target location will receive signals with considerable strength. However, with the decision fusion model 2, when the fraction of mobile nodes,  $\lambda_m$  is increasing the performance gain over a stationary network becomes significant.

Figure 7 shows the variation of overall detection probability with the system false alarm probability  $\alpha_2$  (ROC: receiver operating characteristics) with two decision fusion models for  $\lambda_m = 1/3$  with different delay constraints. Other relevant parameters have the same values as in Fig. 6. As can be seen from Fig.

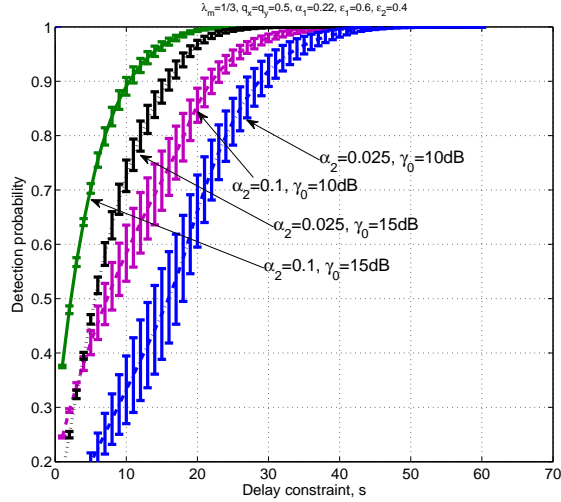


Fig. 8. Deviation of the detection performance due to unavailability of the exact target location:  $T_s = 1s$ ,  $\bar{v} = 1m/s$ ,  $\gamma_0 = 10dB$ ,  $p = 0$ ,  $\alpha_1 = 0.22$ ,  $\lambda_m = 1/6$ ,  $\epsilon_1 = 0.6$ ,  $\epsilon_2 = 0.4$

7, the fusion model 1 outperforms the model 2 especially when the delay constraint is relatively large. It also can be seen that for a given delay constraint and for moderate values of system f.a.p.  $\alpha_2$ , the model 1 outperforms model 2. However, both schemes show similar performance when  $\alpha_2$  is getting large which intuitively makes sense.

Figure 8 shows the deviation of the detection performance due to the averaging strategy used in developing local decisions in this paper. The curves in Fig. 8 correspond to the performance deviation by applying the decision fusion architecture 1 if the target happens to appear at  $(x_a, y_a)$  when  $\gamma_0$  and  $\alpha_2$  are varying. From Fig. 8, it can be seen that for relatively large  $\gamma_0$  the deviation in detection performance is almost negligible. For moderate values of  $\gamma_0$ , it is seen that the deviation in detection performance is not very small, but not too large as well. Note that when the local nodes perform non-coherent detection (unknown target locations), a higher SNR is required to achieve the same performance level compared to that with a coherent detector (known target location) [22]. From the simulation results, it is seen that this deviation is mostly acceptable for a wide range of network parameters.

It is noted that the initial detection performance may affect the distance that the mobile nodes should move in order to achieve a certain desired performance. Figure 9 shows the dependence of the initial detection performance on average moving distance of a mobile node in order to achieve a desired performance. In Fig. 9, we have let the system f.a.p.  $\alpha_2 = 0.1$ ,  $\lambda_m = 1/6$ ,  $q_x = q_y = 0.5$ , local node f.a.p.  $\alpha_1 = 0.22$ . As can be seen from Fig. 9, the initial detection helps to reduce average moving distance of a mobile node specially when the desired detection probability takes moderate values.

In Fig. 10, we compare the detection performance when the node mobility management is performed via dynamic programming approach and the sequential approach. In Fig. 10 we assume that the target



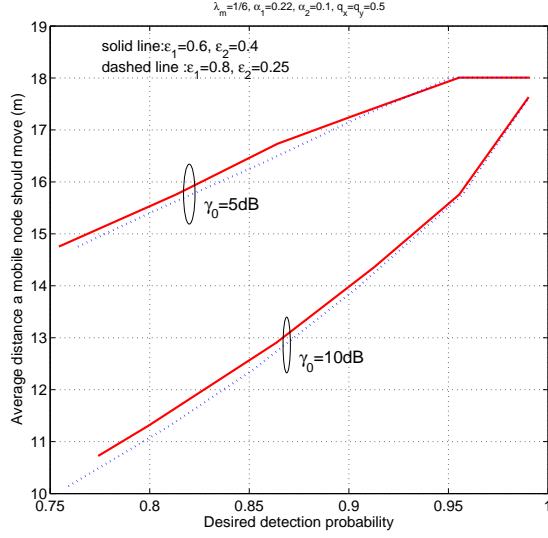


Fig. 9. Dependence of the average distance that a mobile node should move in order to achieve a desired detection probability, on initial detection performance  $\epsilon_1$  and  $\epsilon_2$ ;  $T_s = 1s$ ,  $\bar{v} = 1m/s$ ,  $p_k = p = 0$ ,  $\alpha_1 = 0.22$ ,  $\alpha_2 = 0.1$ ,  $\lambda_m = 1/6$ ,  $q_x = q_y = 0.5$

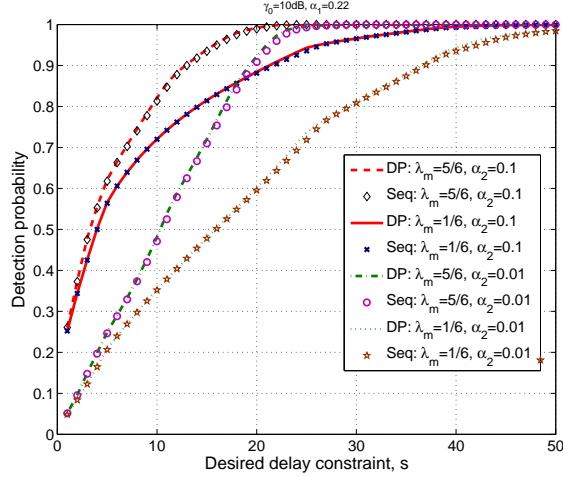


Fig. 10. Comparison of the performance of mobility algorithms based on dynamic programming approach and the sequential approach;  $\epsilon_1 = 0$ ,  $\epsilon_2 = 0$ ;  $T_s = 1s$ ,  $\bar{v} = 1m/s$ ,  $p_k = p = 0$ ,  $\alpha_1 = 0.22$ ,  $\gamma_0 = 10dB$ , target is assumed to be located at  $(0, 0)$

is located at the origin and results correspond to decision fusion model 2. It can be seen from Fig. 10 that when each mobile node uses same speed and same set of direction at each time step, the detection performance with sequential approach fairly matches with that of with the dynamic programming approach. Fig. 10 also depicts that when the desired system f.a.p.  $\alpha_2$  is small, adding mobility greatly improves the detection performance.

In Fig. 11, the minimum fraction of mobile nodes required to achieve a given desired probability at the fusion center is shown when the desired delay constraint  $T_D = 20s$  and  $\alpha_1$  and  $\alpha_2$  are varying. Clearly Fig. 11 shows the trade off between the required number of mobile nodes and the local decision qualities

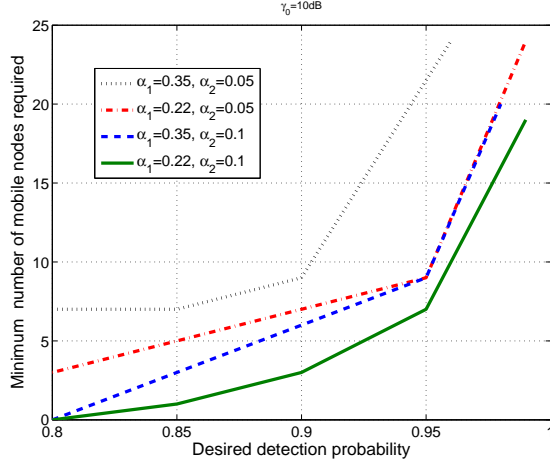


Fig. 11. Minimum number of mobile nodes required to achieve a desired performance level;  $\epsilon_1 = 0$ ,  $\epsilon_2 = 0$ ;  $T_s = 1s$ ,  $\bar{v} = 1m/s$ ,  $p_k = p = 0$ ,  $\gamma_0 = 10dB$ ,  $T_D = 20s$  target is assumed to be located at  $(0, 0)$

when achieving a desired overall system performance level. Thus the Theorem 1 in Section VI is important in determining the required fraction of nodes to be mobile depending on the requirement.

## VIII. CONCLUSION

In this paper, we proposed two decision fusion models for target detection using a hybrid sensor network in which the node mobility is taken into account at node-level and at the fusion center and analyzed the impact of node mobility to the overall performance under both schemes. The mobile nodes in the network are kept stationary until a target is detected with a low confidence level or statistical information on target locations are available and are directed to move to maximize the detection probability during a desired delay constraint once a target is detected within a certain confidence level. We proposed a node mobility management scheme in order to maximize the detection probability within a desired delay constraint. Since deploying mobile nodes in a sensor network is not as cost effective as deploying static nodes, we evaluate the cost of allowing nodes to be mobile in terms of the minimum number of mobile nodes required to achieve a desired performance level within desired delay constraint.

## APPENDIX A

*Proof: (Proposition 1)* Average false alarm probability corresponding to the decision rule (8) at the  $k$ -th mobile node is given by,

$$\bar{P}_{f_k}^m(nT_s) = Pr(\bar{z}_k(n-1, n) \geq \tau_k^m(n) | H_0), \quad (47)$$

where  $\bar{z}_k(n-1, n) = \int_{(n-1)T_s}^{nT_s} z_k(t) \overline{m_k(t)} dt$ . Under  $H_0$  we can show that  $\bar{z}_k(n-1, n)$  is distributed as,

$$\bar{z}_k(n-1, n) | H_0 \sim \mathcal{N}(0, \sigma_u^2 E_k^{\bar{m}}(n-1, n))$$

where  $E_k^{\bar{m}}(n-1, n) = \int_{(n-1)T_s}^{nT_s} \bar{m}_k^2(t) dt$ . Then the false alarm probability (47) becomes,

$$\bar{P}_{f_k}^m(nT_s) = Q\left(\frac{\tau_k^m(n)}{\sigma_u \sqrt{E_k^{\bar{m}}(n-1, n)}}\right). \quad (48)$$

If the allowable false alarm probability at the  $k$ -th mobile node is  $\alpha_1$ , the threshold  $\tau_k^m(n)$  is given by,

$$\tau_k^m(n) = \sigma_u Q^{-1}(\alpha_1) \sqrt{E_k^{\bar{m}}(n-1, n)}. \quad (49)$$

The detection probability at the  $k$ -th mobile node at time  $nT_s$  based on the decision rule (8) is given by,

$$\bar{P}_{d_k}^m(nT_s) = Pr(\bar{z}_k(n-1, n) \geq \tau_k^m(n) | H_1), \quad (50)$$

Under  $H_1$ , conditioned on  $(x_0, y_0)$ ,  $\bar{z}_k(n-1, n)$  is distributed as,

$$\begin{aligned} & \bar{z}_k(n-1, n) | (H_1, x_0, y_0) \\ &= \int_{(n-1)T_s}^{nT_s} m_k(t; x_0, y_0) \bar{m}_k(t) dt + \int_{(n-1)T_s}^{nT_s} \bar{m}_k(t) u_k(t) dt \\ &\sim \mathcal{N}\left(\tilde{E}_k(x_0, y_0; n-1, n), \sigma_u^2 E_k^{\bar{m}}(n-1, n)\right) \end{aligned}$$

where  $\tilde{E}_k(x_0, y_0; n-1, n) = \int_{(n-1)T_s}^{nT_s} m_k(t; x_0, y_0) \bar{m}_k(t) dt$ . Thus the pdf of  $\bar{z}_k(n-1, n)$  under  $H_1$  is given by,

$$\begin{aligned} p_{\bar{Z}_k}(\bar{z}_k) | H_1 &= \mathbb{E}_{x_0, y_0} \{p(\bar{z}_k | H_1, x_0, y_0)\} \\ &= \mathbb{E}_{x_0, y_0} \left\{ \mathcal{N}(\tilde{E}_k(x_0, y_0; n-1, n), \sigma_u^2 E_k^{\bar{m}}(n-1, n)) \right\} \end{aligned}$$

Note that we use  $\bar{z}_k = \bar{z}_k(n-1, n)$  for simplicity, when there is no ambiguity.

Then the detection probability (50) at the  $k$ -th mobile node is given by,

$$\begin{aligned} \bar{P}_{d_k}^m(nT_s) &= \int_{\tau_k^m(n)}^{\infty} p_{\bar{Z}_k}(\bar{z}_k | H_1) d\bar{z}_k \\ &= \int_{\tau_k^m(n)}^{\infty} \mathbb{E}_{x_0, y_0} \left\{ \mathcal{N}(\tilde{E}_k(x_0, y_0; n-1, n), \sigma_u^2 E_k^{\bar{m}}) \right\} d\bar{z}_k \\ &= \mathbb{E}_{x_0, y_0} \left\{ \int_{\tau_k^m(n)}^{\infty} \mathcal{N}(\tilde{E}_k(x_0, y_0; n-1, n), \sigma_u^2 E_k^{\bar{m}}) d\bar{z}_k \right\} \\ &= \mathbb{E}_{x_0, y_0} \left\{ Q\left(\frac{\tau_k^m(n) - \tilde{E}_k(x_0, y_0; n-1, n)}{\sigma_u (E_k^{\bar{m}}(n-1, n))^{1/2}}\right) \right\} \\ &= \mathbb{E}_{x_0, y_0} \left\{ Q\left(Q^{-1}(\alpha_1) - \frac{\tilde{E}_k(x_0, y_0; n-1, n)}{\sigma_u (E_k^{\bar{m}}(n-1, n))^{1/2}}\right) \right\}. \end{aligned}$$

■

## APPENDIX B

*Proof: (Proposition 2)* When nodes are static, we have  $m_k(t) = m_k$  for  $(n-1)T_s < t \leq nT_s$ . Then from subsection IV-A we have,  $\bar{E}_k^m = \bar{E}_k^m(n-1, n)|_{m_k(t)=m_k} = \bar{m}_k^2 T_s$  where  $\bar{m}_k^2 = \mathbb{E}_{x_0, y_0}\{m_k^2\}$ ,  $E_k^{\bar{m}} = E_k^{\bar{m}}(n-1, n)|_{m_k(t)=m_k} = T_s \bar{m}_k^2$ , and  $\tilde{E}_k(x_0, y_0; n-1, n) = m_k(x_0, y_0) \bar{m}_k T$ . Then the decision statistic in the decision rule (8) reduces to,

$$\bar{z}_k(n-1, n) = \bar{m}_k \int_{(n-1)T_s}^{nT_s} z_k(t) dt \quad (51)$$

and the threshold is given by  $\tau_k^s(n) = \tau_k^s = \sigma_u^2 \eta_k^s + \frac{1}{2} \bar{m}_k^2 T_s$  where  $\eta_k^s$  is found such that  $P_{f_k}^s = \alpha_1$ . The false alarm probability associated with the decision rule (8) for the  $k$ -th static node reduces to

$$\bar{P}_{f_k}^s(nT_s) = Q\left(\frac{\tau_k^s}{\sigma_u \bar{m}_k \sqrt{T_s}}\right),$$

To achieve  $\bar{P}_{f_k}^s(nT_s) = \alpha_1$ , the threshold  $\tau_k^s$  can be computed as,  $\tau_k^s = Q^{-1}(\alpha_1) \sigma_u \bar{m}_k \sqrt{T_s}$ . Then the corresponding detection probability (10) for the  $k$ -th static node reduces to,

$$\bar{P}_{d_k}^s(nT_s) = \mathbb{E}_{x_0, y_0} \left\{ Q\left(Q^{-1}(\alpha_1) - \frac{m_k(x_0, y_0) \sqrt{T_s}}{\sigma_u}\right) \right\}, \quad (52)$$

for  $k \in \mathcal{V}_s$ , where we use the relations  $\bar{E}_k^m = \bar{m}_k^2 T_s$ ,  $E_k^{\bar{m}} = T_s \bar{m}_k^2$  and  $\tilde{E}_k(x_0, y_0; n-1, n) = m_k(x_0, y_0) \bar{m}_k T_s$  for static nodes in obtaining (52). ■

## APPENDIX C

### *Proof of theorem 1*

When  $k = 0$ , all mobile nodes are in stationary mode. Then we have,

$$\begin{aligned} K_s(n_D, 0) &= (2\tilde{\rho} + \beta^2) \sum_{j \in \mathcal{V}} P_{d_j}^s(n_D T_s) - \beta^2 \sum_{j \in \mathcal{V}} P_{d_j}^s{}^2(n_D T_s) \\ &\quad - \left( \sum_{j \in \mathcal{V}} P_{d_j}^s(n_D T_s) \right)^2 - \tilde{\rho}^2 \end{aligned} \quad (53)$$

If  $K_s(n_D, 0) \leq 0$ , we have  $f_2(k) - f_1(k) \geq K_s(n_D, k)$  for  $k = 0$  since  $f_2(0) - f_1(0) = 0$  from the definition of  $f_1(\cdot)$  and  $f_2(\cdot)$ . Also from the claim 1 (given below), we can see that then  $f_2(k) - f_1(k) \geq K_s(n_D, k)$  for all  $k \geq 0$ . Then we have  $K_0 = 0$ , where no need for any node to be mobile to achieve the desired performance level within a desired delay constraint. Now, if  $K_s(n_D, 0) > 0$ , in the following we prove that, we can find a unique  $1 \geq K_0 \leq N_m$  such that  $f_2(k) - f_1(k) \geq K_s(n_D, k)$  for  $k \geq K_0$  and  $f_2(k) - f_1(k) < K_s(n_D, k)$  for  $k < K_0$ . The uniqueness of such  $K_0$  is followed from claim 1. If  $f_2(k) - f_1(k) < K_s(n_D, k)$  for all  $k = 1, 2, \dots, N_m$ , it implies that the required performance level can not be achieved within the desired delay constraint even if all mobile nodes are directed to move.

To prove the uniqueness of  $K_0$ , we prove the following.

$$f_2(k+1) - f_1(k+1) \geq K_s(n_D, k+1) + \left( P_{d_{k+1}}^m - P_{d_{k+1}}^s \right) \left[ \beta^2 (P_{d_{k+1}}^m + P_{d_{k+1}}^s - 1) + 2 \left( \sum_{j=1}^{k+1} P_{d_j}^m + \sum_{j \in \mathcal{V}_s^k} P_{d_j}^s - \tilde{\rho} \right) \right] \quad (54)$$

*Claim 1:* If  $f_2(k) - f_1(k) \geq K_s(n_D, k)$  then  $f_2(k+1) - f_1(k+1) \geq K_s(n_D, k+1)$  for  $k = 1, \dots, N_m$ . Also, if  $f_2(k) - f_1(k) \leq K_s(n_D, k)$  we have  $f_2(k-1) - f_1(k-1) \leq K_s(n_D, k-1)$ .

*Proof:* First we prove that if  $f_2(k) - f_1(k) \geq K_s(n_D, k)$  then  $f_2(k+1) - f_1(k+1) \geq K_s(n_D, k+1)$ . Note that, when necessary, we use  $P_{d_k}^s(n_D T_s)$  and  $P_{d_k}^m(n_D T_s)$  to denote the detection probability at the  $k$ -th mobile node at time  $n_D T_s$  at its stationary configuration and mobile configuration, respectively. We have,

$$\begin{aligned} f_2(k+1) - f_1(k+1) &= \left( \sum_{j=1}^{k+1} P_{d_j}^m(n_D T_s) \right)^2 \\ &+ \beta^2 \sum_{j=1}^{k+1} P_{d_j}^{m2}(n_D T_s) + 2 \sum_{j=1}^{k+1} P_{d_j}^m(n_D T_s) \sum_{j \in \mathcal{V}_s^k} P_{d_j}^s(n_D T_s) \\ &- (2\tilde{\rho} + \beta^2) \sum_{j=1}^{k+1} P_{d_j}^m(n_D T_s) \\ &= f_2(k) - f_1(k) + (1 + \beta^2) P_{d_{k+1}}^{m2}(n_D T_s) \\ &+ 2P_{d_{k+1}}^m(n_D T_s) \left( \sum_{j=1}^k P_{d_j}^m(n_D T_s) + \sum_{j \in \mathcal{V}_s^{k+1}} P_{d_j}^s(n_D T_s) \right) \\ &- 2P_{d_{k+1}}^s(n_D T_s) \sum_{j=1}^k P_{d_j}^m(n_D T_s) - (2\tilde{\rho} + \beta^2) P_{d_{k+1}}^m(n_D T_s) \end{aligned} \quad (55)$$

Now adding and subtracting  $K_s(n_D, k)$  to the right hand side of (55), we will get,

$$\begin{aligned} f_2(k+1) - f_1(k+1) &= [f_2(k) - f_1(k) - K_s(n_D, k)] \\ &+ K_s(n_D, k) + (1 + \beta^2) P_{d_{k+1}}^{m2} \\ &+ 2P_{d_{k+1}}^m \left( \sum_{j=1}^k P_{d_j}^m + \sum_{j \in \mathcal{V}_s^{k+1}} P_{d_j}^s \right) \\ &- 2P_{d_{k+1}}^s \sum_{j=1}^k P_{d_j}^m - (2\tilde{\rho} + \beta^2) P_{d_{k+1}}^m \end{aligned} \quad (56)$$

where we dropped argument  $n_D T_s$  such that  $P_{d_k}^s(n_D T_s) = P_{d_k}^s$  and  $P_{d_k}^m(n_D T_s) = P_{d_k}^m$  for simplicity. Substituting for  $K_s(n_D, k)$  from (41) and using the fact that  $f_2(k) - f_1(k) \geq K_s(n_D, k)$ , after simplification (56) reduces to (54).

Note that we use  $P_{d_k}^s(n_D T_s)$  to denote the detection probability at the  $k$ -th mobile node at time  $n_D T_s$  at its stationary configuration, as mentioned before. In (54) Since mobility towards the target improves the detection probability at the  $k$ -th mobile node, we have  $P_{d_{k+1}}^m(n_D T_s) - P_{d_{k+1}}^s(n_D T_s) \geq 0$ . Using this

fact, and with the assumption that  $P_{d_k}^m(n_D T_s), P_{d_k}^s(n_D T_s) \geq \frac{1}{2}$  for  $k \in \mathcal{V}$  (which holds true in practice for sufficient  $n_D T_s$ ) the second term of the right hand side of the inequality (54) is positive. Then we have,

$$f_2(k+1) - f_1(k+1) \geq K_s(n_D, k+1) \quad (57)$$

as required. Following a similar approach, we can prove that  $f_2(k-1) - f_1(k-1) \leq K_s(n_D, k-1)$  if  $f_2(k) - f_1(k) \leq K_s(n_D, k)$ .  $\blacksquare$

## APPENDIX D

### Regularity conditions to apply L-F central limit theorem in subsections IV-C and V-C

Lindeberg-Feller Central Limit Theorem (L-F CLT): Suppose  $S_m = X_1 + \dots + X_m$  is a sum of  $m$  independent random variables with  $\mathbb{E}\{X_k\} = \eta_k$  and  $Var\{X_k\} = \nu_k^2$ . The L-F CLT states that under certain regularity conditions the sum  $S_m$  converges in distribution to a Gaussian random variable with mean  $\sum_{j=1}^m \eta_k$  and the variance  $\sum_{j=1}^m \nu_k^2$  as  $m \rightarrow \infty$  [24]. For the applicability of LF-CLT, it was shown in [25] two sufficient conditions should be satisfied:

- $\nu_k^2 > B_1$
- $\mathbb{E}\{|X_k - \mathbb{E}\{X_k\}|^3\} < B_2$

for  $k = 1, \dots, m$  where  $B_1$  and  $B_2$  are positive values.

To apply the LF-CLT in subsection IV-C, first we prove that the sufficient conditions are satisfied under  $\mathcal{H}_1$  (in the following we assume  $P_D^0 = P_F^0 = 0$  for simplicity). Note that we can write  $\Lambda(nT_s)$  as,

$$\begin{aligned} \Lambda(nT_s) &= \left( \sum_{j=1}^n \sum_{k \in \mathcal{V}_m} w_k(jT_s) + \sum_{j=1}^n \sum_{k \in \mathcal{V}_s} w_k(jT_s) \right) \\ &= \sum_{j,k} X_{j,k}^m + X_{j,k}^s \end{aligned} \quad (58)$$

where  $X_{j,k}^m = w_k(jT_s)$  for  $k \in \mathcal{V}_m$  and  $X_{j,k}^s = w_k(jT_s)$  for  $k \in \mathcal{V}_s$ . Under  $\mathcal{H}_1$ , it can be seen from (13) that  $X_{j,k}^m$  is a Binary random variable with mean  $\mu_{d_k}^m(jT_s)$  and variance  $\mu_{d_k}^m(jT_s)(1 - \mu_{d_k}^m(jT_s))$ . Similarly,  $X_{j,k}^s$  is a Binary random variable with mean  $\mu_{d_k}^s(jT_s)$  and the variance  $\mu_{d_k}^s(jT_s)(1 - \mu_{d_k}^s(jT_s))$ . Then assuming perfect communication channels (such that  $p_k = 0$ ) we have,

$$\begin{aligned} Var(X_{j,k}^m) &= \mu_{d_k}^m(jT_s)(1 - \mu_{d_k}^m(jT_s)) \\ &= P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s)) \end{aligned} \quad (59)$$

and

$$\begin{aligned} \mathbb{E}\{|X_{j,k}^m - \mathbb{E}\{X_{j,k}^m\}|^3\} &= P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s)) \left( P_{d_k}^{m^2}(jT_s) + (1 - P_{d_k}^m(jT_s))^2 \right) \\ &= P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s)) (1 - 2P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s))) \\ &> P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s)) \end{aligned} \quad (60)$$

where last inequality results because  $1 - 2P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s)) < 1$ . Note that from (10), if the local false alarm probability  $\alpha_1$  is set such that  $0 < \alpha_1 < 1$ ,  $P_{d_k}^m(jT_s)$  is positive and finite for any  $j, k$ . Let  $B_1^m = \min_{j,k} \{P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s))\}$  and  $B_2^m = \max_{j,k} \{P_{d_k}^m(jT_s)(1 - P_{d_k}^m(jT_s))\}$ . Then we have  $Var(X_{j,k}^m) > B_1^m$  and  $\mathbb{E}\{|X_{j,k}^m - \mathbb{E}\{X_{j,k}^m\}|^3\} < B_2^m$  for  $j = 1, \dots, n, k \in \mathcal{V}_m$ . Similarly we can show that we can find two positive values  $B_1^s$  and  $B_2^s$  such that  $Var(X_{j,k}^s) > B_1^s$  and  $\mathbb{E}\{|X_{j,k}^s - \mathbb{E}\{X_{j,k}^s\}|^3\} < B_2^s$  for  $j = 1, \dots, n, k \in \mathcal{V}_s$ . Following a similar procedure, it can be shown that the two regularity conditions are satisfied under  $\mathcal{H}_0$  as well.

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