

Properties of Fourier Transforms (know how to derive these)

ECE 433 9/6/07 ①

Linearity:  $a f_1(t) + b f_2(t) \xrightarrow{\mathcal{F}} a F_1(\omega) + b F_2(\omega)$

Convolution:  $f_1(t) * f_2(t) \xrightarrow{\mathcal{F}} F_1(\omega) F_2(\omega)$

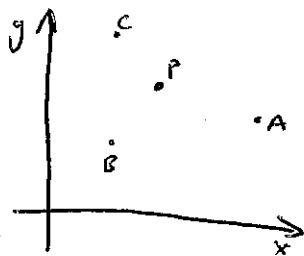
Scaling:  $f(at) \xrightarrow{\mathcal{F}} \frac{1}{|a|} F\left(\frac{\omega}{a}\right)$

Time reversal:  $f(-t) \xrightarrow{\mathcal{F}} F(-\omega)$

Time shift:  $f(t-a) \xrightarrow{\mathcal{F}} e^{-j\omega a} F(\omega)$

Modulation:  $f(t) e^{j\omega_0 t} \xrightarrow{\mathcal{F}} F(\omega - \omega_0)$

# Image Comparison



To test against point a:

$$\|P-a\|_2 = \sqrt{(p_x - a_x)^2 + (p_y - a_y)^2}$$

n-norm

$$\|P-a\|_n = \sqrt[n]{\sum_{i=1}^k (p_i - a_i)^n}$$

not the size of the vector!

vectors are sized k

$$\|P-a\|_1 = |p_x - a_x| + |p_y - a_y|$$

- You can think of <sup>many</sup> images as an  $n$ -dimensional space
- You can apply these kinds of norms