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A PROGRAM FOR COMPUTING NEAR FIELDS
OF THIN WIRE ANTENNAS

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ABSTRACT

A user-oriented computer program is presented and described for analyzing the near fields of thin wire antennas. The program is based on the method of moments and is an extension of a program presented earlier for computing far-field and current distributions. In general the wires of a given configuration can be arbitrarily bent and can be excited or loaded at arbitrary points along their lengths. It is also possible to include wire junctions enabling treatment of special configurations such as wire crosses and supporting wires for long antennas. The subsectional approach used provides accurate results as close as one subsection length from the nearest wire surface.

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I. INTRODUCTION

In this report a method is presented for calculating the near fields of thin wire antennas. The method is based on the reciprocity theorem for electromagnetic fields and can be applied to problems involving thin and arbitrarily bent wires where each wire length L and radius a are such that $L/a \gg 1$ and $a \ll \lambda$, the wavelength. A user-oriented computer program based on this method is presented in the Appendix and instructions for using the program are included in Section IV.

It is assumed here that the current distribution for a given problem is known and furthermore, that it has been computed using a program provided earlier through this project [1]. The portions of that program which are necessary for computing the current corresponding to a given problem geometry are incorporated in the program of the Appendix. These are combined with a subroutine based on the work of Section II that is suitable for computing any given component of the near-zone electric field at any point near the wire structure. (This is subject to a restriction pointed out in the next paragraph.)

The current distribution is computed using the matrix methods suggested by Harrington [2,3]. In order to apply these methods each wire in the problem geometry is thought of as a number of short subsections or segments connected together. The program presented in the Appendix for near-field computations can be expected to provide accurate results up to (but not closer than) a distance equalling the largest of these segment lengths from any wire surface. Work is continuing on modifications that may provide accurate results in closer than this. However, this effort has been hampered by a lack of reliable experimental data corresponding to the regions and structures of interest.

There is another procedure, based on Harrington's work, that is also suitable for near-field computations [4]. A corresponding computer program is available, but not in user-oriented form. However, the method has been used in several instances to verify results obtained with the program of this report.

II. APPROACH BASED ON RECIPROCIITY

For antenna problems the reciprocity theorem states that

$$\int_v \vec{E}_1 \cdot \vec{J}_2 dv = \int_v \vec{E}_2 \cdot \vec{J}_1 dv \quad (1)$$

where \vec{J}_1 and \vec{J}_2 are source current densities, and \vec{E}_1 and \vec{E}_2 are the corresponding electric fields. The reciprocity theorem can be used to find the near field at a given point near a radiating wire structure by considering \vec{J}_1 as the known current on the structure and \vec{J}_2 as the current of an infinitesimal testing dipole placed at the field point in question and oriented with the desired field component. Attention is restricted here to problems involving thin wires where the current of each wire flows only in its axial direction. If ℓ_1 denotes the wire structure and ℓ_2 the testing dipole then (1) can be written as

$$\int_{\ell_2} \vec{E}_1 \cdot I_2 d\vec{\ell}_2 = \int_{\ell_1} \vec{E}_2 \cdot I_1 d\vec{\ell}_1 \quad (2)$$

where I_1 and I_2 are axial currents with directions indicated by $d\vec{\ell}_1$ and $d\vec{\ell}_2$ respectively. For the infinitesimal dipole it is convenient to think of I_2 as constant over ℓ_2 as $\ell_2 \rightarrow 0$. Thus, (2) becomes

$$(E_1)_{\text{along } \ell_2} = \frac{1}{I_2 \ell_2} \int_{\ell_1} \vec{E}_2 \cdot I_1 d\vec{\ell}_1 \quad (3)$$

The current I_1 is known (calculated using the program provided in the Appendix and described earlier [1]) and \vec{E}_2 , the field of the infinitesimal dipole, can be calculated easily. Hence, (3) is a useful starting point from which the desired field components can be found.

\vec{E}_2 can be calculated using the vector and scalar potentials as

$$\vec{E}_2 = -j\omega\mu\vec{A}_2 - \nabla\phi_2 \quad (4)$$

where [5]

$$\vec{A}_2 = \frac{I_2\vec{\ell}_2}{4\pi R} e^{-jkR} \quad (5)$$

$$\phi_2 = -\frac{1}{j\omega\epsilon} \nabla \cdot \vec{A}_2 = \frac{I_2 e^{-jkR}}{4\pi j\omega\epsilon R} \left\{ \frac{1}{R} + jk \right\} \vec{\ell}_2 \cdot \hat{R} \quad (6)$$

and where $k = 2\pi/\lambda$. R is the distance from the source to the field point in question and \hat{R} is its associated unit vector. Substituting (4) - (6) into (3) and integrating by parts yields

$$(E_1)_{\text{along } \ell_2} = \frac{1}{I_2\ell_2} \left\{ -j\omega\mu \int_{\ell_1} I_1 \vec{A}_2 \cdot \vec{d}\ell_1 + \int_{\ell_1} \phi_2 \frac{dI_1}{d\ell_1} d\ell_1 \right\} \quad (7)$$

where use has been made of the fact that the current vanishes at the ends of the wires.

In employing Harrington's matrix methods to determine the current of a thin-wire antenna a series of triangle expansion functions has been used resulting in a piecewise linear approximation to the current. This is illustrated in Fig. 1. It was mentioned earlier that each wire is thought

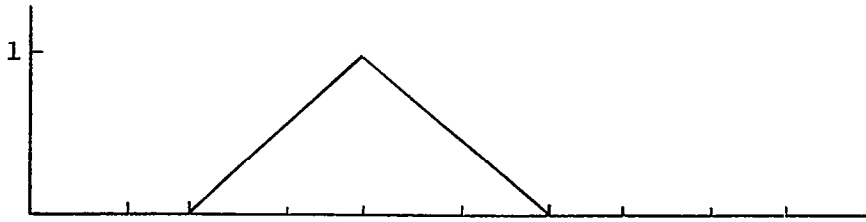


Fig. 1a - Triangle function.

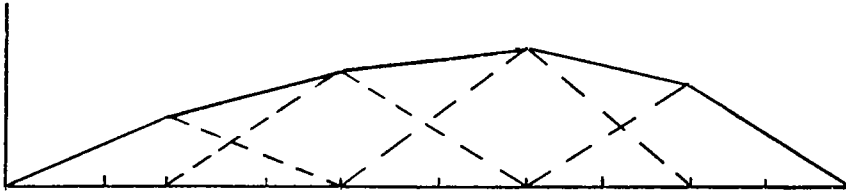


Fig. 1b - Piecewise linear current approximation.

of as a number of short segments connected together, and it is noted that each triangle function extends over four adjacent segments. It is evident then that an even number of segments is required for each wire. The total number of expansion functions for a given problem is denoted by NE. The computer program presented earlier [1] and repeated in the Appendix for convenience calculates amplitudes of these triangles which determine the approximate current distribution. It has been shown through a large number of examples [1,6,7] that current can be determined very accurately in this manner for a wide variety of problems of practical interest.

The expansion of the current for the wire structure is

$$I_1 = \sum_{n=1}^{NE} I'_n T_n \quad (8)$$

where T_n is the nth triangle expansion function and I'_n is its complex amplitude. Inserting (8) in (7) results in

$$(E_1)_{\text{along } \ell_2} = \frac{1}{2\ell_2} \left\{ -j\omega\mu \sum_{n=1}^{NE} \int_{\ell_1} I'_n T_n \vec{A}_2 \cdot \vec{d}\ell_1 + \sum_{n=1}^{NE} \int_{\ell_1} \phi_2 I'_n \frac{dT_n}{d\ell_1} d\ell_1 \right\} \quad (9)$$

In order to simplify the integrations required in (9) each triangle expansion function is approximated by four pulse functions $P_1 \rightarrow P_4$ as shown in Fig. 2. The pulses approximating the nth triangle are denoted by $P_{n1} \rightarrow P_{n4}$. Each pulse function exists over only one segment and its amplitude is simply the average of the triangle function over that segment. Note that the segment lengths are not necessarily all the same. Similarly, the derivative term $dT_n/d\ell_n$ is represented by four pulses $Q_1 \rightarrow Q_4$ as shown also in Fig. 2. These representations allow the integrations of (9) to be written as

$$\int_{\ell_1} I_n' T_n \vec{A}_2 \cdot d\ell_1 \approx I_n' \sum_{i=1}^4 P_{ni} \int_{\Delta\ell_{ni}} \vec{A}_2 \cdot d\ell_{ni} \quad (10)$$

$$\int_{\ell_1} \phi_2 I_n' \frac{dT_n}{d\ell_1} d\ell_1 \approx I_n' \sum_{i=1}^4 Q_{ni} \int_{\Delta\ell_{ni}} \phi_2 d\ell_{ni}$$

Then, using (5) and (6) for \vec{A}_2 and ϕ_2 , (10) becomes

$$\int_{\ell_1} I_n' T_n \vec{A}_2 \cdot d\ell_1 \approx I_2 I_n' \sum_{i=1}^4 P_{ni} (\vec{\ell}_2 \cdot \hat{\ell}_{ni}) \int_{\Delta\ell_{ni}} \frac{e^{-jkR}}{4\pi R} d\ell_{ni} \quad (11)$$

$$\int_{\ell_1} \phi_2 I_n' \frac{dT_n}{d\ell_1} d\ell_1 \approx \frac{I_2 I_n'}{j\omega\epsilon} \sum_{i=1}^4 Q_{ni} (\vec{\ell}_2 \cdot \hat{R}_{ni}) \int_{\Delta\ell_{ni}} \left\{ \frac{e^{-jkR}}{4\pi R^2} + jk \frac{e^{-jkR}}{4\pi R} \right\} d\ell_{ni}$$

where $\hat{\ell}_{ni}$ is a unit vector indicating the direction of the segment corresponding to P_{ni} , and \hat{R}_{ni} is a unit vector directed from the center of that segment to the field point in question. Using (11) with (9),

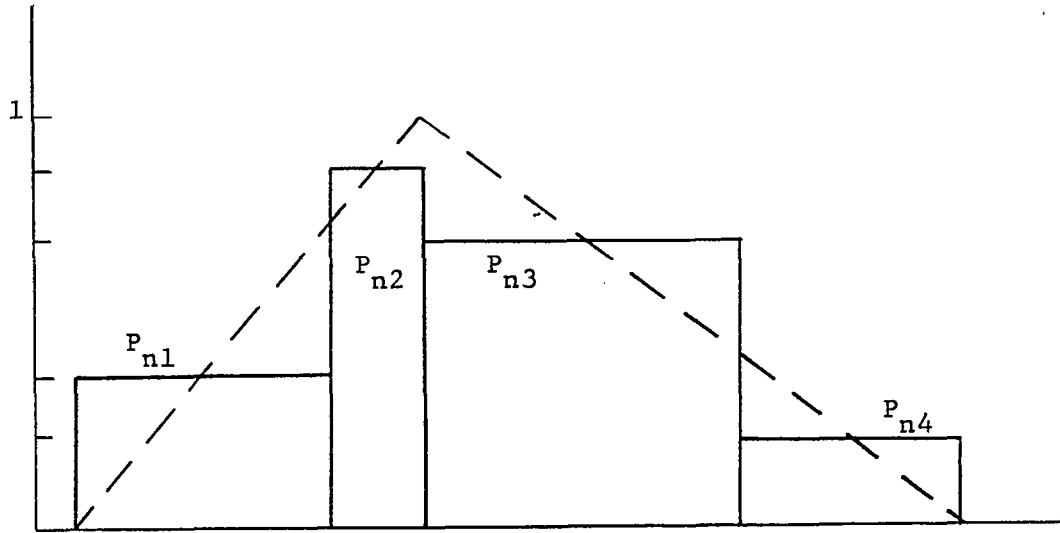


Fig. 2a - Pulses approximating the nth triangle.

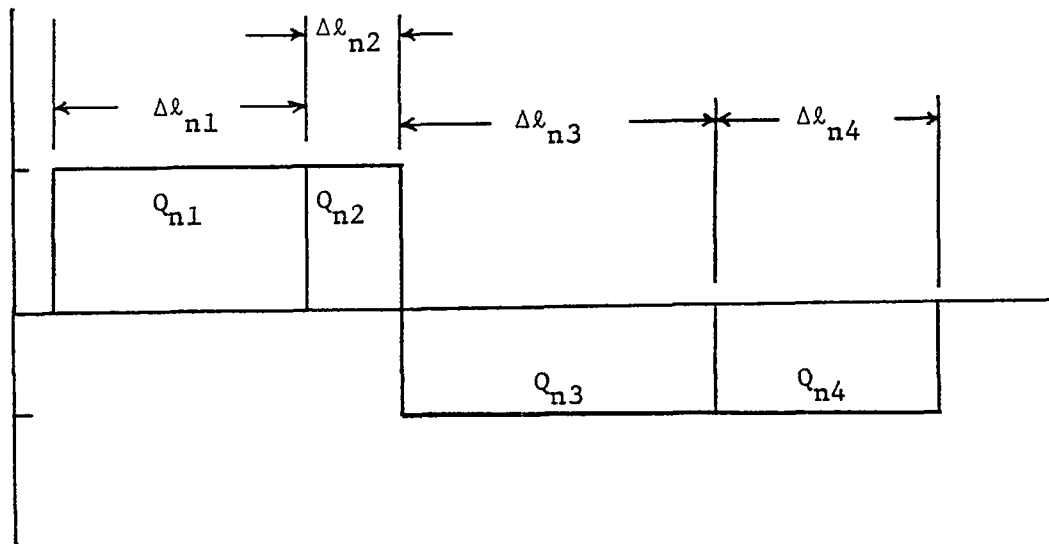


Fig. 2b - Pulses representing the derivative.

$$\begin{aligned}
(E_1)_{\text{along } \hat{\ell}_2} \approx & -j\omega\mu \sum_{n=1}^{NE} I'_n \sum_{i=1}^4 P_{ni} (\hat{\ell}_2 \cdot \hat{\ell}_{ni}) \psi_{ni} \\
& + \frac{1}{j\omega\epsilon} \sum_{n=1}^{NE} I'_n \sum_{i=1}^4 Q_{ni} (\hat{\ell}_2 \cdot \hat{R}_{ni}) (\psi_{ni} + jk\psi'_{ni}) \quad (12)
\end{aligned}$$

where $\hat{\ell}_2$ is a unit vector corresponding to $\vec{\ell}_2$ and

$$\begin{aligned}
\psi_{ni} &= \int_{\Delta \ell_{ni}} \frac{e^{-jkR}}{4\pi R} d\ell_{ni} \\
\psi'_{ni} &= \int_{\Delta \ell_{ni}} \frac{e^{-jkR}}{4\pi R^2} d\ell_{ni} \quad (13)
\end{aligned}$$

The function ψ_{ni} can be evaluated easily using formulas provided by Harrington [2,3]. ψ'_{ni} is calculated in essentially the same way except that more terms must be included in the series expansion of the integrand. Thus, (12) can be used to find the component of \vec{E}_1 in the direction denoted by $\hat{\ell}_2$. This enables computations of the near field of any given thin-wire structure, subject to the conditions (or restrictions) pointed out in Section I.

III. WIRE CURRENT, EXCITATION, LOADING

It was mentioned earlier that the current distribution of a wire structure is expanded in a series of triangle functions resulting in a piecewise linear current approximation. The computed current is printed out as a sequence of complex numbers, each representing the amplitude of a triangle expansion function. These numbers can be arranged as a column matrix of dimension M where M is the total number of expansion functions used. Hence, the current matrix [I] is

$$[I] = \begin{bmatrix} I'_1 \\ I'_2 \\ \vdots \\ I'_M \end{bmatrix} \quad (14)$$

This is related to the excitation voltages applied to the wire structure by

$$[I] = [Z]^{-1}[V] \quad (15)$$

where $[V]$ is a column matrix of M excitation voltages and $[Z]$ is a generalized impedance matrix. The typical element of $[V]$, say V_i , is the complex excitation voltage applied at a position corresponding to the peak of the i th triangle function. If no excitation is applied at that point then the corresponding element of $[V]$ is zero. It should be recognized that this allows excitation voltages to be applied at any arbitrary points on the wire structure since both the number of expansion functions and the lengths of the individual segments used are selected by the program user. Thus, given the excitation voltages, the current for a given problem is computed using (15). Elements of $[Z]$ are computed from general formulas provided by Harrington [2,3] and programmed earlier [1].

Wire loading is handled by defining a diagonal $M \times M$ load impedance matrix $[Z_\ell]$. The typical element $(Z_\ell)_{jj}$ is the complex load impedance in ohms placed at a position corresponding to the peak of the j th triangle function. Of course, if the wire structure is unloaded at that point $(Z_\ell)_{jj}$ is zero. The matrix $[Z_\ell]$ is then simply added to the generalized impedance matrix and the current is given by

$$[I] = [[Z] + [Z_\ell]]^{-1}[V] \quad (16)$$

Then, once the current is known the near-zone fields at points of interest can be computed using the procedures outlined in Section II.

IV. DESCRIPTION OF THE PROGRAM

Subject to the restriction pointed out in Section I the computer program presented in the Appendix is suitable for calculating the components of the electric field vector at any given point in the near field of a thin-wire antenna. The program is written in Fortran IV for use with an IBM 360/50 computer. Complex variables are used to simplify the programming and use is made of a common region to conserve memory space. Sample input and output data are included in the Appendix along with the program listing.

This program is limited to problems involving thin wires with lumped sources and/or lumped loads at wire positions corresponding to the peaks of triangle expansion functions. The maximum number of wires that can be handled is four. The maximum number of expansion functions for any one wire is fifteen. For antennas having more wires or longer wires requiring additional expansion functions to obtain a good current approximation, the dimension statements should be changed. All input data are provided for in the main program, as there are no read statements in the subroutines. All FORMAT statements are placed at the end of the main program.

In this section information is given which should enable the reader to apply the program to specific problems of interest. Particular attention is given to required input data.

DATA INPUT

The first data statement reads in the wavelength in meters, denoted by WAVE in the computer program.

The second data statement reads in the total number of wires in the problem geometry. This is denoted by NWIRE in the program.

The remaining read statements are included in DO Loop 550. This loop iterates a total of NWIRE times. Hence the set of read statements included also executes NWIRE times. Therefore, these five read statements

correspond to NWIRE sets of data cards, with each set corresponding to one wire of the total in the problem geometry.

The third read statement reads in $BA(NW)$, $NS(NW)$, $NF(NW)$, and $NL(NW)$ where NW is the index of DO Loop 550. $BA(NW)$ is the wire radius in wavelengths of the NW th wire. $NS(NW)$ is the number of segments making up the NW th wire. (NS should be an even number.) $NF(NW)$ is the number of feed points on the NW th wire; i.e., the number of segments to which excitation voltages are applied. (If no excitation is applied on the wire, $NF(NW) = 1$ and the source is specified as a source with zero voltage.) $NL(NW)$ is the number of loads on the NW th wire. (If no loads are used on the wire then $NL(NW) = 1$ and the load is specified as $ZL(1,1) = (0.0, 0.0)$, a load with zero impedance.)

The fourth read statement reads in the positions of the feed points on the NW th wire. For example, if excitation voltages are applied to the peaks of the third and eighth triangle functions on the NW th wire then $IF(NW,1) = 3$ and $IF(NW,2) = 8$.

The fifth read statement reads in the applied excitation voltages at the feed points which are specified by the fourth data statement as discussed above.

The sixth read statement provides the positions of the loads along the NW th wire. Thus if the first load on the NW th wire is applied at the peak of the fifth triangle function, the second to the eighth, etc., then $LP(NW,1) = 5$, $LP(NW,2) = 8$, and so on.

The seventh read statement reads in the load impedances to be applied on the NW th wire at the points specified by the sixth data statement. These are written as complex numbers, in ohms.

The next task is to specify the geometry. In the first place, all antennas including those with junctions are treated as combinations of open-ended wires. Hence, the number of expansion functions on the NW th wire can be evaluated as

$$NE(NW) = NS(NW)/2 - 1 \quad (17)$$

and the number of points on the axis of the wire which should be specified can be evaluated as

$$NP(NW) = NS(NW) + 1 \quad (18)$$

$[X(1,NW,I), X(2,NW,I), X(3,NW,I)]$ corresponds to the Cartesian coordinates of the point $P_{NW,I}$ which is the i th point on the NW th wire. The point specifying the geometry of a wire should begin at one end and proceed with consecutive numbering to the last point at the other end of the wire. These points can either be specified by reading in their coordinates or by calculating them with a generating function. In the sample program printout in the Appendix DO Loops 1510 and 1520 are used to specify points on the axis of a single straight wire. These, of course, could just as well be read in point by point as data input. Generating functions for certain other commonly encountered configurations are included in an earlier report [1].

DO Loop 560 obtains XX , XD , and $TLEN$, where the numbers XX are the coordinates of the center points of the segments, XD are the direction numbers of the segments, and $TLEN$ are the lengths of the segments.

The generalized impedance matrix $[Z]$ is computed using subroutine CALZ. Modification of the matrix $[Z]$ to include the effects of loads on the wires is performed by subroutine CALZL. The generalized admittance matrix $[Y]$ is obtained by inverting the matrix $[Z]$ using subroutine LINEQ. (Because we store $[Y]$ and $[Z]$ in the same locations, the admittance matrix is still named $[Z]$ in the program.) The generalized voltage matrix $[V]$ (denoted by $[U]$ in the program) is evaluated using subroutine BIGV. Once the matrices $[Z]^{-1}$ and $[V]$ are available, the generalized current matrix $[I]$ can be obtained by performing the matrix product in subroutine CRNT. DO Loop 30 computes the magnitude and phase of the current and prints them out along with the real and imaginary parts. Each complex number, of course, represents the amplitude of the corresponding triangle expansion function.

Once the current is known all that remains is to specify points at which the near-zone field is to be evaluated and also the particular vector

components to be computed. With regard to the latter suppose vector components denoted by unit vectors $\hat{u}_1, \hat{u}_2, \hat{u}_3$ are desired. This information is read in using a 3x3 matrix YD defined as

$$YD = \begin{bmatrix} \hat{u}_x \cdot \hat{u}_1 & \hat{u}_x \cdot \hat{u}_2 & \hat{u}_x \cdot \hat{u}_3 \\ \hat{u}_y \cdot \hat{u}_1 & \hat{u}_y \cdot \hat{u}_2 & \hat{u}_y \cdot \hat{u}_3 \\ \hat{u}_z \cdot \hat{u}_1 & \hat{u}_z \cdot \hat{u}_2 & \hat{u}_z \cdot \hat{u}_3 \end{bmatrix} \quad (19)$$

Thus, if it is desired to compute the x,y,z components of the electric field at given points then YD is simply a unit matrix. On the other hand if spherical components corresponding to unit vectors $u_r, \hat{u}_\theta, \hat{u}_\phi$ are of interest then

$$YD = \begin{bmatrix} \sin \theta \cos \phi & \cos \theta \cos \phi & -\sin \phi \\ \sin \theta \sin \phi & \cos \theta \sin \phi & \cos \phi \\ \cos \theta & -\sin \theta & 0 \end{bmatrix} \quad (20)$$

Elements of YD are read in with statements 446-454 in the printout shown in the Appendix.

Subroutine ENEAR is used to calculate the near field at given points of interest. The subroutine is called once for each point specified and uses (12) to compute the three vector components desired as described above. The x,y,z coordinates of a given point for which the field is to be computed are labeled YY(1), YY(2), and YY(3) respectively in the program, and these, of course, must be provided by the user. If the field is to be calculated at more than one point then YY(1), YY(2), and YY(3) must be changed for each new point considered. This is done using DO Loop 71 in the program and sample output of the Appendix. Finally, for each point considered the real and imaginary parts, magnitude, and phase of each component of the electric field vector are printed out.

V. EXAMPLES

As an example consider a centered, straight cylindrical antenna that is two meters long and driven by an independent voltage source of two volts. Suppose the wavelength is $4\pi/3$ meters and that the wire radius is constant at 0.00325λ . (This is equivalent to the base-driven monopole studied by Harrison et al. [8].) Suppose further that the wire is unloaded and that a total of 28 segments corresponding to 13 current expansion functions are to be used in the analysis.

The required data input for this problem is as follows:

WAVE = 4.14879 (wavelength in meters)	1st statement
NWIRE = 1 (number of wires)	2nd statement
BA(1) = 0.00325 (radius of first wire in wavelengths)	} 3rd statement
NS(1) = 28 (number of segments - first wire)	
NF(1) = 1 (number of feed points - first wire)	
NL(1) = 1 (number of load positions - first wire)	
IF(1,1) = 7 (first feed point on the first wire is located at the peak of the 7th triangle)	4th statement
V(1,1) = (2.0, 0.0) (excitation applied at the first feed point of the first wire is 2.0 +j0.0)	5th statement
LP(1,1) = 1 (the first load position on the first wire corresponds to the peak of the first triangle)	6th statement
ZL(1,1) = (0.0, 0.0) (load impedance applied at the first load position of the first wire is 0.0 +j0.0)	7th statement

The problem geometry is read in by specifying points along the axis of the wire using DO Loop 1520 and DO Loop 1510. A total of 29 points are used to define the 28 segments making up the wire. In this example all segments are of equal length. Of course, if a generating function is not used to define the problem geometry the axial points can be read in one by one as data input.

Suppose the x, y, z components of the near-zone electric field are of interest. Then the YD matrix is simply a 3×3 unit matrix and is given in statements 446-454 in the program of the Appendix. Finally, DO Loop 71 is used to specify points in space where the near-zone electric field is to be determined. In order to insure accurate results the nearest point, of course, cannot be closer than $\Delta l = 2/28$ meters from the wire surface. In this case the points examined are in the planes defined by $z=0$, $z=0.5$, and $z=1.0$ (where the wire is z -directed with the feed point at $z=0$) and at distances from the wire given by $x=0$ and $y=0.2, 0.6, 1.0, 1.4$ meters. Results are included in the Appendix and these compare quite favorably with those derived earlier by Harrison et al. [8] for $\beta h = 1.5$.

As a second example consider a circular loop antenna located in the xy plane and centered at the origin as shown in Fig. 3. The wire radius is 0.00106λ and the loop radius is $b = \lambda/2\pi$. The wavelength is 0.5 meter and the excitation is a unit voltage at $\phi' = 0$. The problem is treated as an open wire with two segments overlapping at the ends of the wire as explained in the previous report [1]. A total of 30 segments are used, corresponding to 14 current expansion functions. The wire is unloaded and the excitation is applied at a wire position corresponding to the peak of the 14th triangle ($\phi' = 0$).

Input and output data for this problem are included in the Appendix. The problem geometry is defined by specifying positions for a total of 31 points using DO Loops 1510 and 1511. Rectangular near-field vector components are called for so YD is a unit matrix as before. Points at which the field is to be calculated are read in using DO Loop 71. These are shown in the printout of the Appendix to be along the x -axis at $x=0.0, 0.02, 0.06, 0.14, 0.30, \text{ and } 0.62$.

Examples involving use of more than one wire, bent and loaded wires, and wire junctions are available elsewhere [1]. Data for these can be used directly with the program presented here. The only additional input required are the YD matrix and the locations of points where near-field computations are to be made.

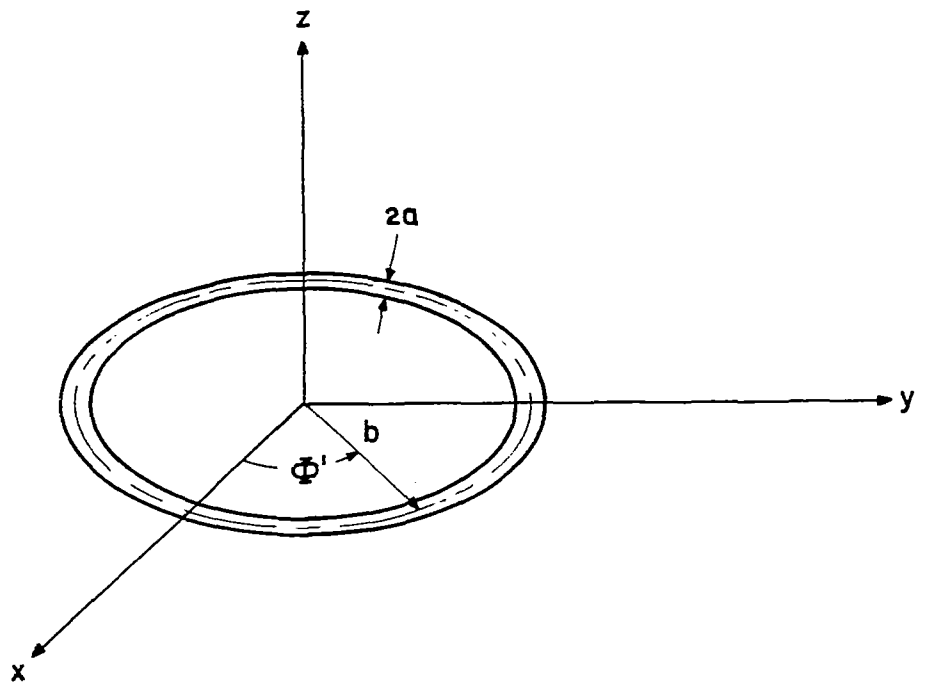


Fig. 3a - Circular loop and coordinate system.

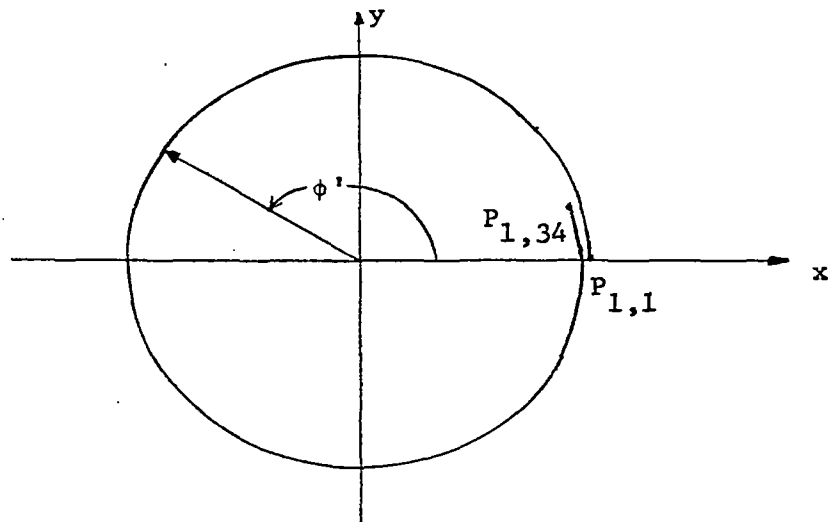


Fig. 3b - Open wire with two segments overlapping.

VI. CONCLUSION

A user-oriented computer program has been presented and described for calculating the near fields of thin wire antennas. The program is an extension of one presented earlier for computing current distributions and far-field patterns for arbitrary configurations of bent wires with junctions. Results are valid for a given point in space if the point is at least a distance Δl from the nearest wire surface, where Δl denotes the length of the longest subsection or segment used in the analysis. The wires of a given problem can be excited or loaded at arbitrary points along their lengths, and no unrealistic assumptions are necessary regarding their current distributions. Finally, mutual coupling is taken completely into account with each step of the analysis procedure.

In this report instructions for using the program were given with particular attention devoted to required data input. Two examples were included to illustrate its use.

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VIII. APPENDIX

This program is suitable for computing near fields of thin wires with excitations represented by lumped voltage sources at the peaks of the triangle functions and loading represented by lumped loads, also at the peaks of the triangle functions. The maximum number of wires that can be handled here is four. The maximum number of expansion functions for any wire is fifteen. Subroutines are listed first. The sample input and output data listed here correspond to the analysis of example one. The problem geometry is read in with instructions 402-415. The YD matrix is provided through instructions 446-454 and field points of interest are specified with statements 456-480. The program is described in Section IV.

```

1      SUBROUTINE ENEAR (WAVE,NWIRE,A,NE,C,NEP,YY,YD)
2      COMPLEX PSI(4),PSI1(4),CI,RT,EX(3,60),C(60),E(3),Z1,Z2
3      I,CMPLX,HOLD1,HOLD2,CEXP
4      DIMENSION YY(3),YD(3,3),NE(NWIRE),YDD(3,4),XDD(3,4),RX(3),A(4),
5      IP(4),Q(4),XD(3,4,32),XX(3,4,32),TLEN(4,32)
6      COMMON /CDA/XX,XD,TLEN /CDE/F
7      CI=(0.,1.)
8      PI=3.14159265
9      BETA=2.0*PI/WAVE
10     EPSLN=8.854E-12
11     DMEG=2.0*PI*2.997923E8/WAVE
12     XMU=4.0E-7*PI
13     N=0
14     DO 10 NWS=1,NWIRE
15     NENWS=NF(NWS)
16     DO 10 NES=1,NENWS
17     N=N+1
18     IF (NES.EQ.1) GO TO 11
19     PSI(1)=PSI(3)
20     PSI(2)=PSI(4)
21     PSI1(1)=PSI1(3)
22     PSI1(2)=PSI1(4)
23     DO 191 I=1,3
24     XDD(I,1)=XDD(I,3)
25     XDD(I,2)=XDD(I,4)
26     YDD(I,1)=YDD(I,3)
27     YDD(I,2)=YDD(I,4)
28     191 CONTINUE
29     KK=3
30     GO TO 18
31     11 KK=1
32     18 CONTINUE
33     DO 60 K=KK,4

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```

32      NESK=2*NES-2+K
33      R=0.
34      DO 15 J=1,3
35      RX(J)=XX(J,NWS,NFSK)-YY(J)
36      15 R=R+RX(J)**2
37      R=SQRT(R)
38      DO 192 I=1,3
39      XDD(I,K)=0.
40      YDD(I,K)=0.
41      DO 100 J=1,3
42      XDD(I,K)=XDD(I,K)+Y(J,I)*RX(J)/R
43      YDD(I,K)=YDD(I,K)+X(J,NWS,NFSK)*YD(J,I)
44      100 CONTINUE
45      192 CONTINUE
46      ALP=TLN(NWS,NESK)/2.
47      ZZ=0
48      DO 33 J=1,3
49      33 ZZ=ZZ+RX(J)*XD(J,NWS,NESK)/(2.*ALP)
50      ZZ=ABS(ZZ)
51      AL=SQRT(ABS(R**2-ZZ**2))
52      IF(R.GE.10.*ALP) GO TO 31
53      RT=COS(-BETA*R)+CI*SIJ(-BETA*R)
54      ZA=ZZ+ALP
55      ZAM=Z-ALP
56      SZA=SQRT(AL**2+ZA**2)
57      SZAM=SQRT(AL**2+ZAM**2)
58      IF(ZZ.GT.ALP) GO TO 41
59      A11=ALOG((ZA+SZA)*(-ZAM+SZAM)/AL**2)
60      GO TO 42
61      41 A11=ALOG((ZA+SZA)/(ZAM+SZAM))
62      42 A12=2.*ALP
63      A13=(ZA*SZA-ZA11*SZAM+AL**2*A11)/2.
64      A14=A12*AL**2+(2.*ALP**3+5.*AL**2*ZZ**2)/3.
65      PSIA=A11-BETA**2/2.*(A13-2.*R**2+R**2*A11)
66      PSIB=-BETA*(A12-R*A11)+BETA**3/6.*(A14-3.*R**2*A13+3.*R**2*A12-R**4
1*A11)
67      PSI(K)=RT/(3*PI*ALP)*CMPLX(PSIA,PSIB)
68      R2=R**2
69      R3=R**3
70      R4=R**4
71      ARG=2.*AL*ALP/(R**2-ALP**2)
72      A10=ATAN(ARG)/AL
73      PSIC=A10-BETA**2/2.*(A12-2.*R**2*A11+R**2*A11)+BETA**4/24.*(A14-4.*R
1*A13+5.*R**2*A12-4.*R**3*A11+R**4*A10)
74      PSD0=-BETA*(A11-R*A10)+BETA**3/6.*(A13-3.*R**2*A12+5.*R**2*A11
1-R**3*A10)
75      PSI1(K)=RT/(3*PI*ALP)*CMPLX(PSIC,PSI0)+CI*BETA*PSI(K)
76      GO TO 59
77      31 XKD=BETA*ALP
78      RT=COS(-BETA*R)+CI*SIJ(-BETA*R)
79      Z1=ZZ/R
80      DR=ALP/R
81      ZR2=ZR**2
82      ZR4=ZR2**2

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83      DR2=DR**2
84      H=(-1.0+3.0*ZR2)/6.0
85      H1=(3.0-30.0*ZR2+35.0*ZR4)/40.0
86      A0=1.0+H*DR2+H1*DR2**2
87      A1=H*DR+H1*DR2*DR
88      A2=-ZR2/6.0-DR2/40.0*(1.0-12.0*ZR2+15.0*ZR4)
89      A3=DR/50.0*(3.0*ZR2-5.0*ZR4)
90      A4=ZR4/120.0
91      PSIA=A0+XKD**2*A2+XKD**4*A4
92      PSIB=XKD*A1+XKD**3*A3
93      PSI(K)=RT/(4.*PI*K)*CMPLX(PSIA,PSIB)
94      B0=1.+DR2*(-1.+4.*ZR2)/3.+2*DR2**2*(1.-12.*ZR2+16.*ZR4)
95      H1=DR*(-1.+5.*ZR2)/5.+0.025*(5.-66.*ZR2+93.*ZR4)*DR**3
96      B2=-ZR2/6.-0.025*DR2*(1.-18.*ZR2+29.*ZR4)
97      B3=DR/50.0*(3.*ZR2-7.*ZR4)
98      B4=A4
99      PSIC=30+XKD**2*B2+XKD**4*B4
100     PSID=XKD*B1+XKD**3*B3
101     PSI1(K)=PT/(4.*PI**4**2)*CMPLX(PSIC,PSID)+CI*BETA*PSI(K)
102     59 CONTINUE
103     60 CONTINUE
104     M=2*NES-2
105     ABCA=TLEN(NWS,2*NES-1)
106     ABCB=TLEN(NWS,2*NES)
107     ABCC=TLEN(NWS,2*NES+1)
108     ABCD=TLEN(NWS,2*NES+2)
109     P(1) = 1/2.*ABCA/(ABCA+ABCB)
110     P(2) = (ABCA+1/2.*ABCB)/(ABCA+ABCB)
111     P(3) = (1/2.*ABCC+ABCD)/(ABCC+ABCD)
112     P(4) = 1/2.*ABCD/(ABCC+ABCD)
113     Q(1) = 1./(ABCA+ABCB)
114     Q(2)=Q(1)
115     Q(3) =-1./(ABCC+ABCD)
116     Q(4)=Q(3)
117     DO 190 I=1,3
118     Z1=0
119     Z2=0
120     DO 193 J=1,4
121     Z1=Z1+P(J)*PSI(J)*YJD(I,J)
122     193 Z2=Z2+Q(J)*PSI1(J)*XJD(I,J)*TLEN(NWS,M+J)
123     EX(I,N)=-CI*OMEG*XMJ*Z1*CN -CI/(OMEG*EPSLN)*Z2*CN)
124     190 CONTINUE
125     10 CONTINUE
126     DO 70 I=1,3
127     E(I)=(0.,0.)
128     DO 70 N=1,NEP
129     E(I)=F(I) + EX(I,N)
130     70 CONTINUE
131     RETURN
132     END

```



```

133     SUBROUTINE CALZ( WAVE,NWIRE,A,NE,NN)
134     COMPLEX Z(60,60),Z+(4,15,4,15),PSI(4,32,4)
135     I,RT, CEXP, CI, C,PLX, HULD1, HULD2
136     DIMENSION A(NWIRE),NE(NWIRE),NN(NWIRE),XX(3,4,32),
137     IXD(3,+,32), TLEN(4,32), R(4,32,4),RX(3,4,32,4),
138     ZZZ(4,32,4), XDD(4,32,4),ALP(4),C(4),D(4),P(4),Q(4)
139     COMMON /CJA/ XX,XD,TLEN /CJB/ Z
140     CI=(0.0,1.0)
141     PI=3.14159265
142     BETA=2.0*PI/WAVE
143     EPSLN = 8.354E-12
144     UMEG = 2.0*PI*2.997928E8/WAVE
145     XMU=4.0E-7*PI
146     DO 10 NWS=1,NWIRE
147     NENWS=NE(NWS)
148     DO 10 NES=1,NE,NWS
149     C NWS= THE NUMBER OF THE WIRE (SOURCE)
150     C NWF= THE NUMBER OF THE WIRE (FIELD POINT)
151     C NES = THE NUMBER OF THE EXPENSION FUNCTION (SOURCE)
152     C NEF = THE NUMBER OF THE EXPENSION FUNCTION (FIELD POINT)
153     C NSS = THE NUMBER OF THE SEGMENT (SOURCE)
154     C NSF = THE NUMBER OF THE SEGMENT (FIELD POINT)
155     IF(NES.EQ.1) GO TO 11
156     DO 17 NWF=1,NWIRE
157     NNNWF=NN(NWF)
158     DO 17 NSF=1,NNNWF
159     XDD(NWF,NSF,1) = XDD(NWF,NSF,3)
160     XDD(NWF,NSF,2) = XDD(NWF,NSF,4)
161     PSI(NWF,NSF,1) = PSI(NWF,NSF,3)
162     17 PSI(NWF,NSF,2) = PSI(NWF,NSF,4)
163     KK = 3
164     GO TO 18
165     11 KK=1
166     18 CONTINUE
167     DO 60 K =KK,4
168     NESK=2*NES-2+K
169     DO 60 NWF=1,NWIRE
170     NNNWF=NN(NWF)
171     DO 60 NSF=1,NNNWF
172     R(NWF,NSF,K) = 0.
173     DO 15 J=1,3
174     RX(J,NWF,NSF,K) = XX(J,NWF,NSF) - XX(J,NWS,NESK)
175     15 R(NWF,NSF,K) = R(NWF,NSF,K) + RX(J,NWF,NSF,K)**2
176     R(NWF,NSF,K) = SQRT(R(NWF,NSF,K))
177     ALP(K) = TLEN(NWS,NESK)/2.
178     ZZ(NWF,NSF,K) = 0.
179     DO 33 J=1,3
180     33 ZZ(NWF,NSF,K) = ZZ(NWF,NSF,K)+RX(J,NWF,NSF,K)*XD(J,NWS,NESK)/
181     I(2.*ALP(K))
182     ZZ(NWF,NSF,K) = ABS(ZZ(NWF,NSF,K))
183     XDD(NWF,NSF,K)=0.
184     DO 65 J=1,3
185     65 XDD(NWF,NSF,K) = XDD(NWF,NSF,K)+XD(J,NWS,NESK ) *XD(J,NWF,NSF)
186     AL = SWFT(ABS(X(NWF,NSF,K)**2-ZZ(NWF,NSF,K)**2))

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177     AL=SQRT(AL**2+A(NWS)**2)
178     IF (R(NWF,NSF,K).GE.10.*ALP(K)) GO TO 31
179     R(NWF,NSF,K) = SQRT(R(NWF,NSF,K)**2+A(NWS)**2)
180     RT = COS(-BETA*R(NWF,NSF,K)) + CI*SIN(-BETA*R(NWF,NSF,K))
181     ZA = ZZ(NWF,NSF,K) + ALP(K)
182     ZAM = ZZ(NWF,NSF,K)-ALP(K)
183     SZA=SQRT(AL**2+ZA**2)
184     SZAM=SQRT(AL**2+ZAM**2)
185     IF (ZZ(NWF,NSF,K).GT.ALP(K)) GO TO 41
186     AI1=ALOG((ZA+SZA)*(-ZAM+SZAM)/AL**2)
187     GO TO 42
41     AI1=ALOG((ZA+SZA)/(ZAM+SZAM))
42     AI2=2.*ALP(K)
190     AI3=(ZA*SZA-ZAM*SZAM+AL**2*AI1)/2
191     AI4=AI2*AL**2+(2.*ALP(K)**3+6.*ALP(K)*ZZ(NWF,NSF,K)**2)/3.
192     PSI1=AI1-BETA**2/2.*(AI3-2.*R(NWF,NSF,K)*AI2+R(NWF,NSF,K)**2*AI1)
193     PSI2= -BETA*(AI2-R(NWF,NSF,K)*AI1)+BETA**3/6.*(AI4-3.*R(NWF,NSF,K)
194     I*AI3+3.*R(NWF,NSF,K)**2*AI2-R(NWF,NSF,K)**3*AI1)
195     PSI(NWF,NSF,K) = RT/(8*PI*ALP(K))*CMLPX(PSI1,PSI2)
196     GO TO 59
31     XKD=BETA*ALP(K)
197     RT = COS(-BETA*R(NWF,NSF,K)) + CI*SIN(-BETA*R(NWF,NSF,K))
198     ZR=ZZ(NWF,NSF,K)/R(NWF,NSF,K)
199     DR=ALP(K)/R(NWF,NSF,K)
200     ZR2=ZR**2
201     ZR4=ZR2**2
202     DR2=DR**2
203     H=(-1.0+3.0*ZR2)/6.0
204     H1=(3.0-30.0*ZR2+35.0*ZR4)/40.0
205     A0=1.0+H*DR2+H1*DR2**2
206     A1=H*DR+H1*DR2*DR
207     A2=-ZR2/6.0-DR2/40.0*(1.0-12.0*ZR2+15.0*ZR4)
208     A3=DR/60.0*(3.0*ZR2-5.0*ZR4)
209     A4=ZR4/120.0
210     PSI1=A0+XKD**2*A2+XKD**4*A4
211     PSI2=XKD*A1+XKD**3*A3
212     PSI(NWF,NSF,K) = RT/(4*PI*R(NWF,NSF,K))*CMLPX(PSI1,PSI2)
59     CONTINUE
60     CONTINUE
215     ABCA=TLEN(NWS,2*NES-1)
216     ABCB=TLEN(NWS,2*NES)
217     ABCC=TLEN(NWS,2*NES+1)
218     ABCD=TLEN(NWS,2*NES+2)
219     C(1) = 1/2.*ABCA/(ABCA+ABCB)
220     C(2) = (ABCA+1/2.*ABCB)/(ABCA+ABCB)
221     C(3) = (1/2.*ABCC+ABCD)/(ABCC+ABCD)
222     C(4) =1/2.*ABCD/(ABCC+ABCD)
223     D(1) = 1./(ABCA+ABCB)
224     D(2) =D(1)
225     D(3) =-1./(ABCC+ABCD)
226     D(4) =D(3)
227     DO 10 NWF=1,NWIRE
228     NENWF=NE(NWF)
229     DO 10 NES=1,NENWF
230     ABCA=TLEN(NWF,2*NES-1)

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231      ABCB=TLEN(NWF,2*NEF)
232      ABCC=TLEN(NWF,2*NEF+1)
233      ABCD=TLEN(NWF,2*NEF+2)
234      P(1) = 1/2.*ABCA/(ABCA+ABCB)
235      P(2) = (ABCA+1/2.*ABCB)/(ABCA+ABCB)
236      P(3) = (1/2.*ABCC+ABCD)/(ABCC+ABCD)
237      P(4) =1/2.*ABCD/(ABCC+ABCD)
238      Q(1) = 1./(ABCA+ABCB)
239      Q(2) = Q(1)
240      Q(3) =-1./(ABCC+ABCD)
241      Q(4) =Q(3)
242      Z4(NWF,NEF,NWS,NES) = (0.,0.)
243      DO 70 I=1,4
244      DO 70 K=1,4
245      L=2*NEF-2+I
246      70 Z4(NWF,NEF,NWS,NES) = Z4(NWF,NEF,NWS,NES) + CI*OMEG*XMJ*C(K)*P(I)*
      IXDU(NWF,L,K)*PSI(NWF,L,K)+1./(CI*OMEG*EPSLN)*D(K)*Q(I)*PSI(NWF,L,
      2K)*TLEN(NWS,2*NES-2+K)*TLEN(NWF,L)
247      10 CONTINUE
248      NUF =0
249      DO 90 NWF =1,NWIRE
250      NENWF=NE(NWF)
251      DO 90 NEF=1,NENWF
252      NUF = NUF +1
253      NUS = 0
254      DO 90 NWS=1,NWIRE
255      NENWS=NE(NWS)
256      DO 90 NES=1,NENWS
257      NUS = NUS+1
258      90 Z(NUF,NUS) = Z4(NWF,NEF,NWS,NES)
259      RETURN
260      END
C      ////////////////////////////////////////////////////
261      .      SUBROUTINE CALZL(NL,NE,NWIRE)
C      TO ADD THE IMPEDANCE MATRIX ZL TO Z TO FORM THE TOTAL IMPEDANCE
C      MATRIX
C      Z=THE IMPEDANCE MATRIX
C      ZL = LOADS
C      NE IS NUMBER OF EXPANSION FUNCTIONS
C      NWIRE = NUMBER OF WIRES
C      COMPLEX Z(50,60),ZL(4,32)
262      DIMENSION LP(4,32) ,NL(NWIRE),NE(NWIRE)
263      COMMON /CJ3/ Z /COC/ZL,LP
264      JJ=0
265      DO 20 K=1,NWIRE
266      IF (K.EQ.1) GOTO 11
267      JJ=JJ+NE(K-1)
268      11 CONTINUE
269      NLK=NL(K)
270      DO 20 I=1,NLK
271      J=JJ+LP(K,I)
272      20 Z(J,J)=Z(J,J)+ZL(K,I)
273      RETURN
274      END
275

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276      SUBROUTINE LINEQ(N, L,M)
C      USE GAUSS-JORDAN METHOD
C      N=ORDER OF THE MATRIX
C      A=THE INPUT AND OUTPUT MATRIX
C      L,M=WORKING VECTOR
277      COMPLEX      A(60,60),BIGA,HOLD
278      DIMENSION L(N),A(N)
279      COMMON /CUB/ A
280      DO 80 K=1,N
281      L(K)=K
282      M(K)=K
283      BIGA=A(K,K)
284      DO 20 J=K,N
285      DO 20 I=K,N
286      10 IF (CABS(BIGA)-CABS(A(I,J))) 15,19,19
287      15 BIGA=A(I,J)
288      L(K)=I
289      M(K)=J
290      19 CONTINUE
291      20 CONTINUE
292      J=L(K)
293      IF(J-K) 35,35,25
294      25 CONTINUE
295      DO 30 I=1,N
296      HOLD=-A(K,I)
297      A(K,I)=A(J,I)
298      30 A(J,I)=HOLD
299      35 I=M(K)
300      IF(I-K) 45,45,38
301      38 CONTINUE
302      DO 40 J=1,N
303      HOLD=-A(J,K)
304      A(J,K)=A(J,I)
305      40 A(J,I)=HOLD
306      45 CONTINUE
307      DO 55 I=1,N
308      IF(I-K) 50,55,50
309      50 A(I,K)=A(I,K)/(-BIGA)
310      55 CONTINUE
311      DO 65 I=1,N
312      DO 65 J=1,N
313      IF(I-K) 60,64,60
314      60 IF(J-K) 62,64,62
315      62 A(I,J)=A(I,K)*A(K,J)+A(I,J)
316      64 CONTINUE
317      65 CONTINUE
318      DO 75 J=1,N
319      IF(J-K) 70,75,70
320      70 A(K,J)=A(K,J)/BIGA
321      75 CONTINUE
322      A(K,K)=1./BIGA
323      80 CONTINUE
324      K=N
325      100 K=K-1
326      IF(K) 150,150,105
327      105 I=L(K)
328      IF(I-K) 120,120,108
329      108 CONTINUE

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420      DD 560 NW=1,NWIRE
421      NNNW=MIN(NW)
422      DO 15 I=1,N,NNW
423      DU 15 J=1,3
424      XX(J,NW,I) = (X(J,NW,I)+X(J,NW,I+1))/2.
425 15  XD(J,NW,I)=X(J,NW,I+1)-X(J,NW,I)
426      DO 20 I=1,NNW
427      20  TLEN(NW,I) = SQRT(XD(1,NW,I)**2+XD(2,NW,I)**2+XD(3,NW,I)**2)
428      A(NW) = BA(NW)*WAVE
429 560  CONTINUE
430      WRITE(3,151)
431      NEP=0
432      LJ 28 NW=1,NWIRE
433      28  NEP=NEP+NE(NW)
434      CALL CALZ (WAVE,NWIRE,A,NE,NN)
435      CALL CALZL(NL,NE,NWIRE)

436      CALL LINEQ(NEP,LMNJP,MMNJP)
437      CALL BIGV(U,NE,NWIRE,NE,NEP)
438      CALL CRNT(U,C,NEP)
439      WRITE (3,203)
440      WRITE (3,208)
441      DO 29 I=1,NEP
442      CMAG=CABS(C(I))
443      CPHASE= ATAN2(AIMAG(C(I)),REAL(C(I)))*180./3.1416
444      WRITE (3,51) I,C(I), CMAG,CPHASE
445 29  CONTINUE
446      YD(1,1)=1.
447      YD(2,1)=0.
448      YD(3,1)=0.
449      YD(1,2)=0.
450      YD(2,2)=1.
451      YD(3,2)=0.
452      YD(1,3)=0.
453      YD(2,3)=0.
454      YD(3,3)=1.
455      WRITE (3,151)
456      DO 71 M=1,3
457      XM=M
458      DO 71 K=1,7,2
459      XK=K
460      YY(1)=0.
461      YY(2)=0.2*XK
462      YY(3)=(XM-1.)*0.5
463      CALL LINEQ (WAVE,NWIRE,A,NE, C,NEP,YY,YD)
464      E(2)=2.*PI*YY(2)*E(1)
465      E(3)=PI*1.33333333*E(3)
466      WRITE (3,202)
467      WRITE (3,1) YY(1), YY(2), YY(3)
468      WRITE (3,201)
469      WRITE (3,207)
470      JC 27 J=1,3
471      EMAG = CABS ( E(J) )
472      IF (FMAG.LT.0.1E-9) GO TO 16
473      EPHASE = ATAN2(AIMAG(E(J)),REAL(E(J)))*180./3.1416
474      GO TO 17

```

```

475     16 EPHASE=0.
476     17 CONTINUE
477     WRITE (3,51) J,E(J), EMAG,EPHASE
478     27 CONTINUE
479     WRITE (3,152)
480     71 CONTINUE
481     GJ TO 100
482     1 FORMAT ( F10.5,4I5)
483     2 FORMAT (3F10.5)
484     3 FORMAT(16I5)
485     4 FORMAT( 8F10.3)
486     5 FORMAT(' BA=',F10.5,' NS=',I5,' NF=',I5,' NL=',I5)
487     6 FORMAT(' IF(I)=',16I5)
488     7 FORMAT(' V(I)=',8F12.3)
489     8 FORMAT(' LP(I)=', 16I5)
490     9 FORMAT(' ZL(I)=',8F10.3)
491     10 FORMAT (' X=',E10.3,' Y=',E10.3,' Z=', E10.3)
492     11 FORMAT(' WAVE =',F20.5)
493     12 FJRMAT(' NWIRE = ',I5)
494     13 FORMAT(' DATA FOR THE ',I5,'TH WIRE')
495     14 FORMAT (2E10.5)
496     51 FORMAT (I5,3E12.4,F10.3)

497     151 FORMAT(' *****')
498     152 FORMAT(' -----')
499     201 FORMAT(' FIELD')
500     202 FORMAT(' COORDINATES OF TESTING POINT ')
501     203 FORMAT(' CURRENT DISTRIBUTION')
502     207 FORMAT(' J E(J) MAGNITUDE PHASE')
503     208 FORMAT(' I C(I) MAGNITUDE PHASE')
504     300 FORMAT(' ',12E10.2)
505     310 FORMAT(' THE COORDINATE OF THE WIRE')
506     500 STOP
507     END

```

WARNING FORMAT STATEMENT 14 IS UNREFERENCED

```

$DATA
WAVE = 4.14879
NWIRE = 1
*****
DATA FOR THE 1TH WIRE
BA= 0.00325 NS= 28 NF= 1 NL= 1
IF(I)= 7
V(I)= 2.000 0.000
LP(I)= 1
ZL(I)= 0.000 0.000

```

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-----
THE COORDINATE OF THE WIRE
0.00E 00 0.00E 00 -0.10E 01 0.00E 00 0.00E 00 -0.93E 00
0.00E 00 0.00E 00 -0.86E 00 0.00E 00 0.00E 00 -0.79E 00
0.00E 00 0.00E 00 -0.71E 00 0.00E 00 0.00E 00 -0.64E 00
0.00E 00 0.00E 00 -0.57E 00 0.00E 00 0.00E 00 -0.50E 00
0.00E 00 0.00E 00 -0.43E 00 0.00E 00 0.00E 00 -0.36E 00

```


0.00E 00 0.00E 00 -0.29E 00 0.00E 00 0.00E 00 -0.21E 00
 0.00E 00 0.00E 00 -0.14E 00 0.00E 00 0.00E 00 -0.71E-01
 0.00E 00 0.00E 00 0.00E 00 0.00E 00 0.00E 00 0.71E-01
 0.00E 00 0.00E 00 0.14E 00 0.00E 00 0.00E 00 0.21E 00
 0.00E 00 0.00E 00 0.29E 00 0.00E 00 0.00E 00 0.36E 00
 0.00E 00 0.00E 00 0.43E 00 0.00E 00 0.00E 00 0.50E 00
 0.00E 00 0.00E 00 0.57E 00 0.00E 00 0.00E 00 0.64E 00
 0.00E 00 0.00E 00 0.71E 00 0.00E 00 0.00E 00 0.79E 00
 0.00E 00 0.00E 00 0.86E 00 0.00E 00 0.00E 00 0.93E 00

0.00E 00 0.00E 00 0.10E 01

CURRENT DISTRIBUTION

I	C(I)		MAGNITUDE	PHASE
1	0.7150E-02	-0.2666E-02	0.7531E-02	-20.448
2	0.1227E-01	-0.4340E-02	0.1302E-01	-19.471
3	0.1670E-01	-0.5563E-02	0.1750E-01	-18.422
4	0.2029E-01	-0.6286E-02	0.2124E-01	-17.216
5	0.2294E-01	-0.6471E-02	0.2383E-01	-15.754
6	0.2457E-01	-0.6101E-02	0.2531E-01	-13.947
7	0.2512E-01	-0.4439E-02	0.2551E-01	-10.023
8	0.2457E-01	-0.6101E-02	0.2531E-01	-13.947
9	0.2294E-01	-0.6471E-02	0.2333E-01	-15.754
10	0.2029E-01	-0.6286E-02	0.2124E-01	-17.216
11	0.1670E-01	-0.5563E-02	0.1750E-01	-18.422
12	0.1227E-01	-0.4340E-02	0.1302E-01	-19.471
13	0.7150E-02	-0.2666E-02	0.7631E-02	-20.448

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.200E 00 Z= 0.000E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1337E-04	-0.6916E-04	0.7044E-04	-100.944
3	-0.9584E 01	0.1600E 01	0.9717E 01	170.522

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.600E 00 Z= 0.000E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.8707E-05	-0.2803E-04	0.2935E-04	-107.256
3	-0.5035E 01	0.2723E 01	0.5724E 01	151.594

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.100E 01 Z= 0.000E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1685E-04	-0.2551E-04	0.3058E-04	-123.446
3	-0.2924E 01	0.3553E 01	0.4601E 01	129.452

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.140E 01 Z= 0.000E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.2035E-04	-0.5178E-05	0.2100E-04	-165.725
3	-0.8500E 00	0.3685E 01	0.3782E 01	102.988

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.200E 00 Z= 0.500E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1269E 01	-0.6008E 01	0.6141E 01	-101.925
3	-0.4910E 01	-0.1231E 00	0.4912E 01	-178.564

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.600E 00 Z= 0.500E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1405E 01	-0.4528E 01	0.4741E 01	-107.243
3	-0.4671E 01	0.1612E 01	0.4941E 01	160.962

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.100E 01 Z= 0.500E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1675E 01	-0.3163E 01	0.3579E 01	-117.906
3	-0.2781E 01	0.2997E 01	0.4088E 01	132.858

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.140E 01 Z= 0.500E 00

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1972E 01	-0.2043E 01	0.2839E-01	-133.991
3	-0.7754E 00	0.3342E 01	0.3430E 01	104.062

COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.200E 00 Z= 0.100E 01

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1994E 01	-0.5543E 01	0.5891E 01	-109.789
3	-0.9241E 01	-0.1320E 02	0.1612E 02	-124.990

 COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.600E 00 Z= 0.100E 01

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.1987E 01	-0.4594E 01	0.5006E 01	-113.392
3	-0.4485E 01	-0.6136E 00	0.4527E 01	-172.209

 COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.100E 01 Z= 0.100E 01

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.2574E 01	-0.3699E 01	0.4576E 01	-124.837
3	-0.2392E 01	0.1946E 01	0.3083E 01	140.874

 COORDINATES OF TESTING POINT

X= 0.000E 00 Y= 0.140E 01 Z= 0.100E 01

FIELD

J	E(J)		MAGNITUDE	PHASE
1	0.0000E 00	0.0000E 00	0.0000E 00	0.000
2	-0.3205E 01	-0.2507E 01	0.4059E 01	-141.966
3	-0.5492E 00	0.2530E 01	0.2538E 01	102.017

The material that follows corresponds to the circular loop problem of example two. The subroutines are not listed since they are the same as before. The main program is the same as that used for example one except that the problem geometry is different as specified using statements 402-413, and also the field points of interest are different as specified using statements 454-474.

```

C      MAIN PROGRAM                MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
370      COMPLEX ZL(4,32),V(+,32),Z(60,60),U(50),C(60),
      IE(3), ZIN,CDF,JG,C1,YIN,CAI,C3I,CC
371      DIMENSION BA(12),A(12),NS(12),NF(12),NL(12),NCLUSE(12),
      IX(3,4,32),NP(12),NP(12),IN(12),IF(4,32),LP(4,32),XX(3,4,32),
      2XD(3,4,32),TLEN(4,32),LMNUP(60),MMNUP(60),
      3YY(3),YD(3,3)
372      COMMON /CJA/XX,X,TLEN /CIB/Z /CIC/ZL,LP /CID/V,IF /CDE/E
373      PI = 3.14159265
374      XMU = 4.0E-7*PI

375      EPSLN = 8.854E-12
376      CI = (0.,1.)
377      100 READ (1,2, END=500) WAVE
378      WRITE (3,11) WAVE
379      JMPS=2.697723E8/WAVE*2.*PI
380      PETA = 2.*PI/WAVE
381      READ (1,3) NWIRE
382      WRITE (3,12) NWIRE
383      WRITE (3,151)
384      DO 500 NW=1,NWIRE
385      WRITE (3,13) NW
386      READ (1,1) BA(NW),NS(NW),NF(NW),NL(NW)
387      WRITE (3,5) BA(NW),NS(NW),NF(NW),NL(NW)
388      NFNW=NF(NW)
389      READ(1,3) (IF(NW,I),I=1,NFNW )
390      WRITE(3,6) (IF(NW,I),I=1,NFNW )
391      READ (1,4) (V(NW,I),I=1,NFNW )
392      WRITE(3,7) (V(NW,I),I=1,NFNW )
393      NLNW =NL(NW)
394      READ (1,3) (LP(NW,I),I=1,NLNW )
395      WRITE (3,8) (LP(NW,I),I=1,NLNW )
396      READ (1,4) (ZL(NW,I),I=1,NLNW)
397      WRITE(3,9) (ZL(NW,I),I=1,NLNW )
398      WRITE (3,152)
399      NE(NW) = NS(NW)/2-1
400      NP(NW) =NS(NW) +1
401      NN(NW) = 2*NF(NW)+2
402      RID=WAVE/(2.*PI)
403      DPH=2.*PI/(NS(NW)-2)
404      NPNW=NP(NW)-3

```

```

405      DO 1510 I=1, NPNW
406          X(1,NW,I)=R ID*CS(((I-1)*PHI)
407          X(2,NW,I)=R ID*SI(((I-1)*PHI)
408      1510 X(3,NW,I)=0
409          DO 1511 J=1,3
410              NPNW=NPNW
411              X(J,NW,NPNW)=X(J,NW,3)
412              X(J,NW,NPNW-1)=X(J,NW,2)
413      1511 X(J,NW,NPNW-2)=X(J,NW,1)
414              WRITE (3,310)
415              WRITE(3,310) ((X(J,NW,I),J=1,3),I=1,NPNW)
416              WRITE (3,152)
417      550 CONTINUE
418          DO 500 NW=1,NWIRE
419              NPNW=NP(NW)
420              DO 15 I=1,NPNW
421                  DO 15 J=1,3
422                      XX(J,NW,I) = (X(J,NW,I)+X(J,NW,I+1))/2.
423      15  XD(J,NW,I)=X(J,NW,I+1)-X(J,NW,I)
424                  DO 20 I=1,NPNW
425                      20 TLEN(NW,I) = SQRT(XD(1,NW,I)**2+XD(2,NW,I)**2+XD(3,NW,I)**2)
426                      A(NW) = 3A(NW)*WAVL
427      550 CONTINUE
428              WRITE (3,151)
429              NEP=0
430              DO 28 NW=1,NWIRE
431      28  NEP=NEP+NE(NW)
432              CALL CALZ (WAVE, WIRE, A, NE, IN)
433              CALL CALZL(NL,NE,NWIRE)
434              CALL LINEP(NEP,LENP,INJP)
435              CALL FIGV(U,NF,NWIRE,NE,NEP)
436              CALL CPNT(U,C,NEP)
437              WRITE (3,203)
438              WRITE (3,20P)
439              DO 29 I=1,NEP
440                  CMAG=CMAGS(C(I))
441                  CPHASE=ATAN2(AIMAG(C(I)),REAL(C(I))*131.73.1415)
442              WRITE (3,51) I,C(I),CMAG,CPHASE
443      29 CONTINUE
444              YD(1,1)=1.
445              YD(2,1)=0.
446              YD(3,1)=0.
447              YD(1,2)=0.
448              YD(2,2)=1.
449              YD(3,2)=0.
450              YD(1,3)=0.
451              YD(2,3)=0.
452              YD(3,3)=1.
453              WRITE (3,151)
454              DO 71 K=1,5
455                  EK=2.**(K-1)-1.
456                  YY(1)=.02**K
457                  YY(2)=0.
458                  YY(3)=0.
459              CALL EQUAX (WAVE,C,NWIRE,A,NE,C,NFP,YY,YD)

```

```

460      WRITE (3,202)
461      WRITE (3,17) YY(1), YY(2), YY(3)
462      WRITE (3,201)
463      WRITE (3,207)
464      DO 27 J=1,3
465      EMAG = CABS ( E(J) )
466      IF (EMAG.LT.?.1E-9) GO TO 16
467      EPHASE = ATAN2(AIMAG(E(J)),REAL(E(J)))*180./3.1416
468      GO TO 17
469      15 EPHASE=0.
470      17 CONTINUE
471      WRITE (3,51) J,E(J), EMAG,EPHASE
472      27 CONTINUE
473      WRITE (3,152)
474      71 CONTINUE
475      GO TO 100
476      1 FORMAT ( F10.5,4I5)
477      2 FORMAT ( 2F10.5)
478      3 FORMAT(15I5)
479      4 FORMAT( 8F10.3)
480      5 FORMAT(' BA=',F10.5,' NS=',I5,' NF=',I5,' NL=',I5)
481      6 FORMAT(' I(I)=',15I5)
482      7 FORMAT(' V(I)=',8F12.3)
483      8 FORMAT(' LP(I)=',15I5)
484      9 FORMAT(' ZL(I)=',8F10.3)
485      10 FORMAT(' X=',E10.3,' Y=',E10.3,' Z=', F10.3)
486      11 FORMAT(' WAVE =',F20.5)
487      12 FORMAT(' WIRE = ',I5)
488      13 FORMAT(' DATA FOR THE ',I5,'TH WIRE')
489      14 FORMAT (2E10.4)
490      51 FORMAT (I5,3E12.4,F10.3)
491      151 FORMAT(' *****')
492      152 FORMAT(' -----')
493      201 FORMAT(' FIELD')
494      202 FORMAT (' COORDINATES OF TESTING POINT ')
495      203 FORMAT (' CURRENT DISTRIBUTION')
496      207 FORMAT (' J E(J) MAGNITUDE PHASE')
497      208 FORMAT (' I C(I) MAGNITUDE PHASE')
498      300 FORMAT(' ',12E10.2)
499      310 FORMAT(' THE COORDINATE OF THE WIRE')
500      STOP
501      END
**WARNING** FORMAT STATEMENT 14 IS UNREFERENCED

```

```

$DATA
WAVE = 0.50000
NWIRE = 1
*****
DATA FOR THE 1TH WIRE
BA= 0.00106 NS= 30 NF= 1 NL= 1
IF(I)= 14
V(I)= 1.000 0.000
LP(I)= 1
ZL(I)= 0.000 0.000

```

 THE COORDINATE OF THE WIRE

0.80E-01	0.00E 00	0.00E 00	0.78E-01	0.13E-01	1.00E 00	0.72E-01
0.35E-01	0.00E 00	0.62E-01	0.50E-01	0.00E 00		
0.50E-01	0.62E-01	0.00E 00	0.35E-01	0.72E-01	0.00E 00	0.18E-01
0.78E-01	0.00E 00	0.10E-06	0.80E-01	0.00E 00		
-0.16E-01	0.78E-01	0.00E 00	-0.35E-01	0.72E-01	0.00E 00	-0.50E-01
0.62E-01	0.00E 00	-0.62E-01	0.50E-01	0.00E 00		
-0.72E-01	0.35E-01	0.00E 00	-0.78E-01	0.13E-01	1.00E 00	-0.80E-01
0.13E-06	0.00E 00	-0.78E-01	-0.18E-01	0.00E 00		
-0.72E-01	-0.35E-01	0.00E 00	-0.52E-01	-0.50E-01	1.00E 00	-0.50E-01
-0.62E-01	0.00E 00	-0.35E-01	-0.72E-01	0.00E 00		
-0.18E-01	-0.78E-01	0.00E 00	-0.13E-06	-0.80E-01	0.00E 00	0.18E-01
-0.78E-01	0.00E 00	0.35E-01	-0.72E-01	0.00E 00		
0.50E-01	-0.62E-01	0.00E 00	0.52E-01	-0.50E-01	0.00E 00	0.72E-01
-0.35E-01	0.00E 00	0.78E-01	-0.18E-01	0.00E 00		
0.80E-01	0.00E 00	0.00E 00	0.78E-01	0.13E-01	0.00E 00	0.72E-01

 0.50E-01 0.00E 00

CURRENT DISTRIBUTION

I	C(I)		AMPLITUDE	PHASE
1	0.4221E-02	0.3083E-02	0.5227E-12	36.145
2	0.2930E-02	0.1616E-02	0.3346E-12	23.886
3	0.1066E-02	-0.1118E-04	0.1056E-02	-1.601
4	-0.9994E-03	-0.1531E-02	0.1071E-02	-127.295
5	-0.2853E-02	-0.2531E-02	0.4058E-02	-134.774
6	-0.4143E-02	-0.2736E-02	0.5579E-12	-137.957
7	-0.4601E-02	-0.4034E-02	0.6120E-02	-138.757
8	-0.4143E-02	-0.3736E-02	0.5579E-02	-137.955
9	-0.2358E-02	-0.2531E-02	0.4053E-02	-134.769
10	-0.9990E-03	-0.1531E-02	0.1070E-02	-127.283
11	0.1067E-02	-0.1130E-04	0.1057E-02	-1.607
12	0.2930E-02	0.1616E-02	0.3346E-02	23.882
13	0.4221E-02	0.3083E-02	0.5227E-12	36.144
14	0.4682E-02	0.4346E-02	0.6538E-02	42.874

COORDINATES OF TESTING POINT

X= 0.00E 00 Y= 0.00E 00 Z= 0.00E 00

FIELD

J	E(J)		AMPLITUDE	PHASE
1	-0.7919E-04	0.2463E-03	0.2587E-03	107.824
2	-0.6722E 01	0.2178E 01	0.7066E 01	162.042
3	0.0000E 00	0.0000E 00	0.0000E 00	0.000

 COORDINATES OF TESTING POINT

X= 0.200E-01 Y= 0.000E 00 Z= 0.000E 00

FIELD

J	E(J)	MAGNITUDE	PHASE
1	-0.7657E-04	0.2765E-03	106.078
2	-0.7239E 01	0.7538E 01	163.829
3	0.0000E 00	0.0000E 00	0.000

 COORDINATES OF TESTING POINT

X= 0.600E-01 Y= 0.000E 00 Z= 0.000E 00

FIELD

J	E(J)	MAGNITUDE	PHASE
1	0.3620E-04	0.5723E-03	46.381
2	-0.1105E 02	0.1515E 01	172.190
3	0.0000E 00	0.0000E 00	0.000

 COORDINATES OF TESTING POINT

X= 0.140E 00 Y= 0.000E 00 Z= 0.000E 00

FIELD

J	E(J)	MAGNITUDE	PHASE
1	-0.1320E-03	0.1845E-03	-135.676
2	-0.2897E 01	0.2903E 01	-176.295
3	0.0000E 00	0.0000E 00	0.000

 COORDINATES OF TESTING POINT

X= 0.300E 00 Y= 0.000E-00 Z= 0.000E 00

FIELD

J	E(J)	MAGNITUDE	PHASE
1	-0.1414E-04	0.2918E-04	119.000
2	0.1374E 00	0.1272E 01	83.834
3	0.0000E 00	0.0000E 00	0.000

 COORDINATES OF TESTING POINT

X= 0.620E 00 Y= 0.000E 00 Z= 0.000E 00

FIELD

J	E(J)	MAGNITUDE	PHASE
1	-0.1362E-05	0.6130E-05	-102.842
2	-0.4901E 00	0.6193E 00	-142.318
3	0.0000E 00	0.0000E 00	0.000
